

## **0. Introduction**

### **1. Reminder:**

**E-Dynamics in homogenous media and at interfaces**

## **2. Photonic Crystals**

**2.1 Introduction**

**2.2 1D Photonic Crystals**

**2.3 2D and 3D Photonic Crystals**

**2.4 Numerical Methods**

**2.5 Fabrication**

**2.6 Non-linear optics and Photonic Crystals**

**2.7 Quantumoptics**

**2.8 Chiral Photonic Crystals**

**2.9 Quasicrystals**

**2.10 Photonic Crystal Fibers – „Holey“ Fibers**

## **3. Metamaterials and Plasmonics**

**3.1 Introduction**

**3.2 Background**

**3.2 Fabrication**

**3.3 Experiments**

# Bibliography

- **“Optik”, E. Hecht, Addison-Wesley  
(just as a reminder)**
- **“Nanophotonics”, P.N. Prasad, John Wiley & Sons (2004)  
(recent comprehensive overview, nothing in depth,  
good for finding further references and original work)**
- **“Photonic Crystals”, J.D. Joannopoulos, R.D. Meade, J.N. Winn,  
Princeton University Press  
(nice textbook introduction into the theory, mostly 2D)**
- **“Photonic Crystals”, K. Busch et al., eds.,  
Wiley-VCH (2004)  
(collection of recent review papers, incl. experimental ones)**
- **“Optical Properties of Photonic Crystals”, K. Sakoda, Springer (2001)  
(advanced theory, mostly 2D, good introduction into symmetry  
properties)**

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### **3. Metamaterials and Plasmonics**

**3.1 Introduction**

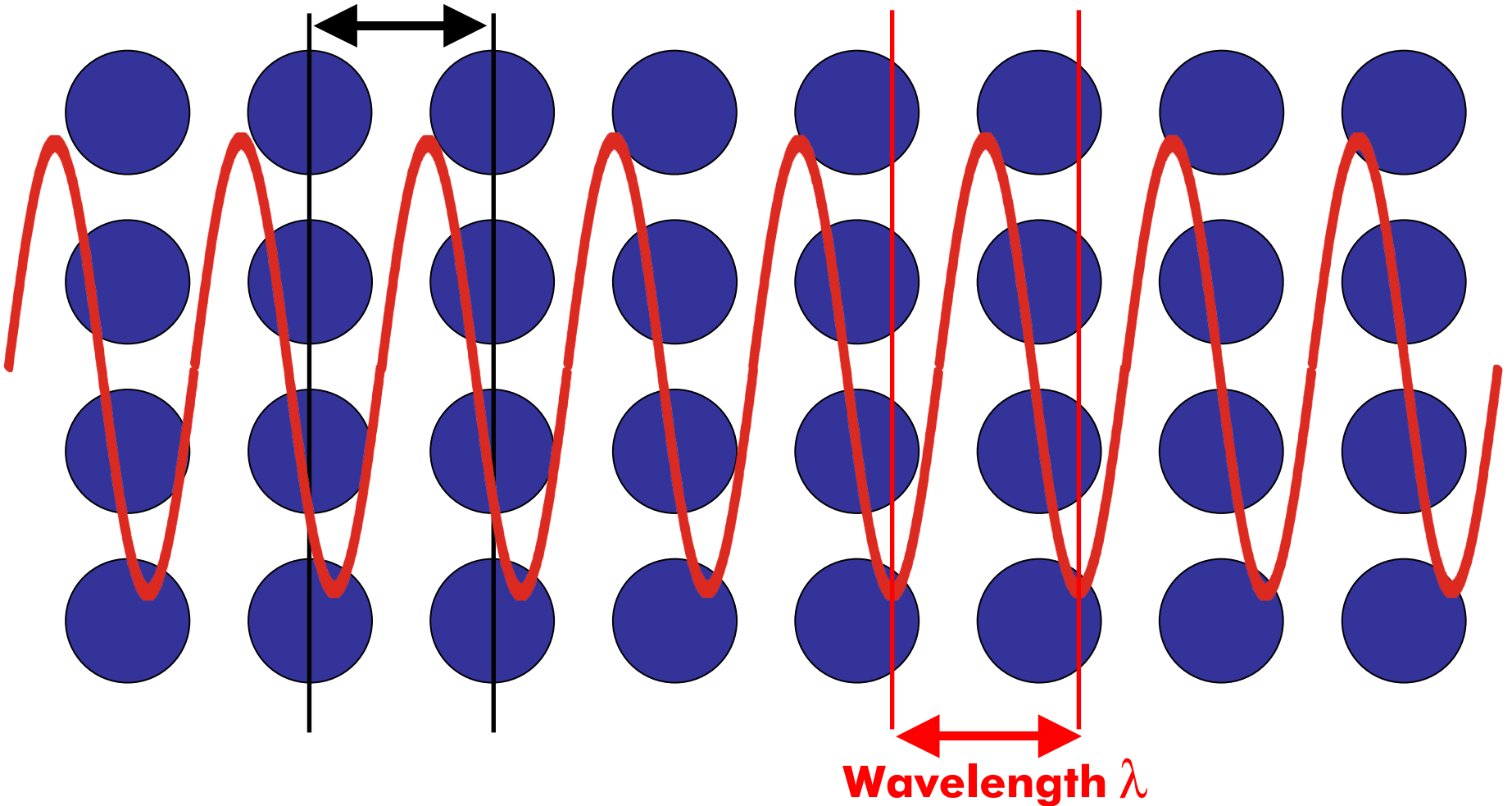
**3.2 Background**

**3.2 Fabrication**

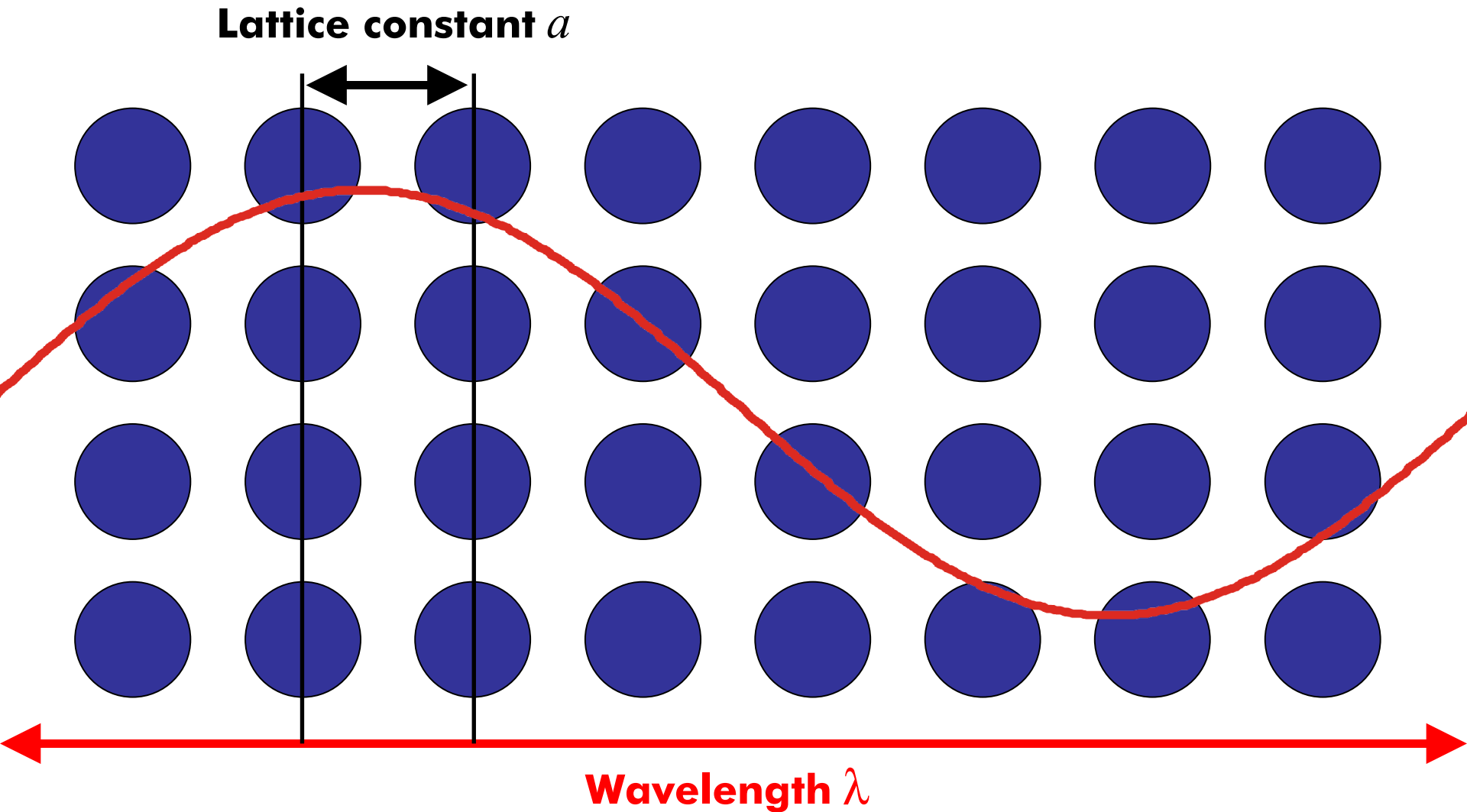
**3.3 Experiments**

# Optical properties of periodic structures

Lattice constant  $a$

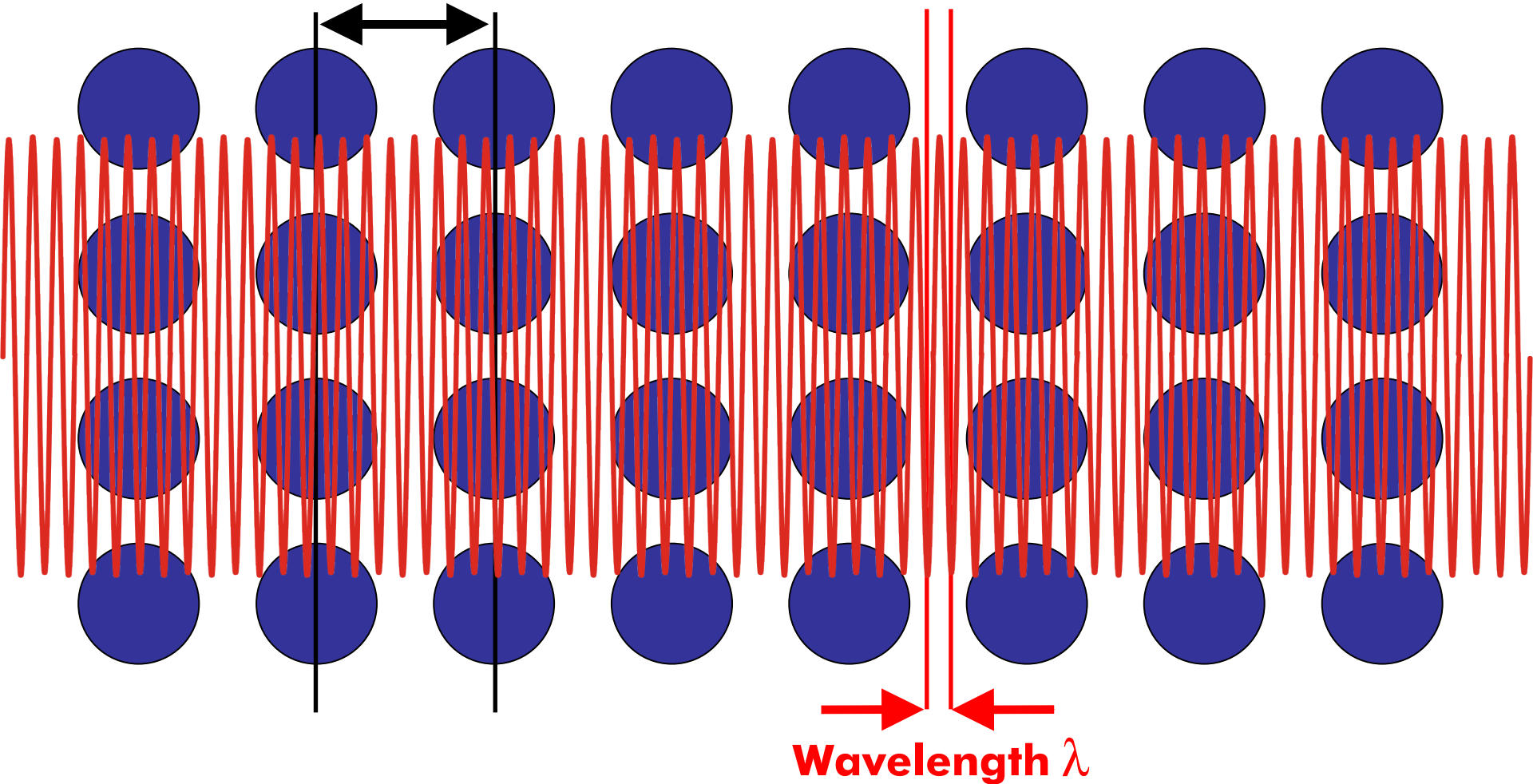


# Optical properties of periodic structures



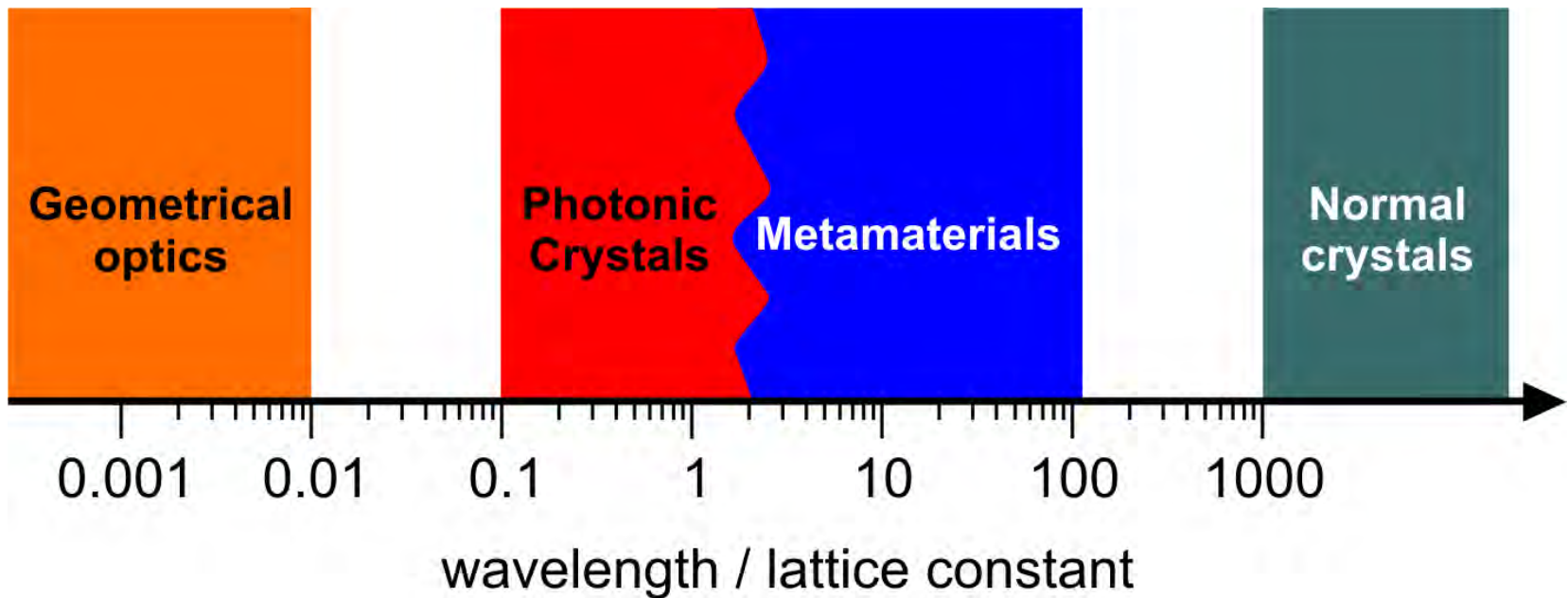
# Optical properties of periodic structures

Lattice constant  $a$

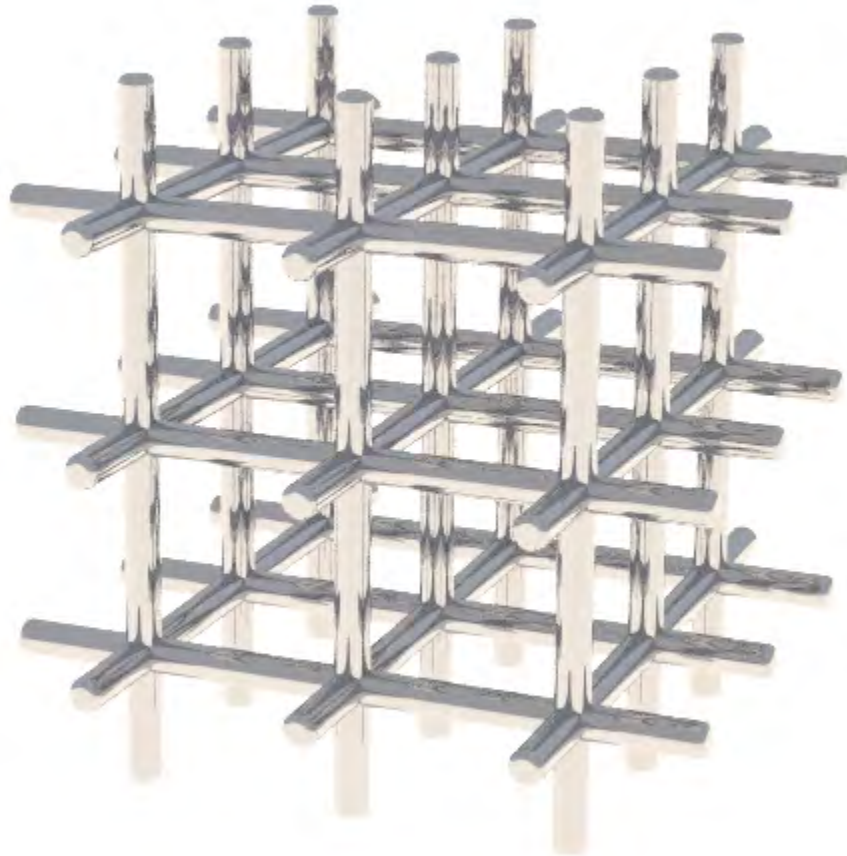


# Theoretical framework

Relevant parameter: wavelength  $\lambda$  / lattice constant  $a$



# Geometrical optics ...



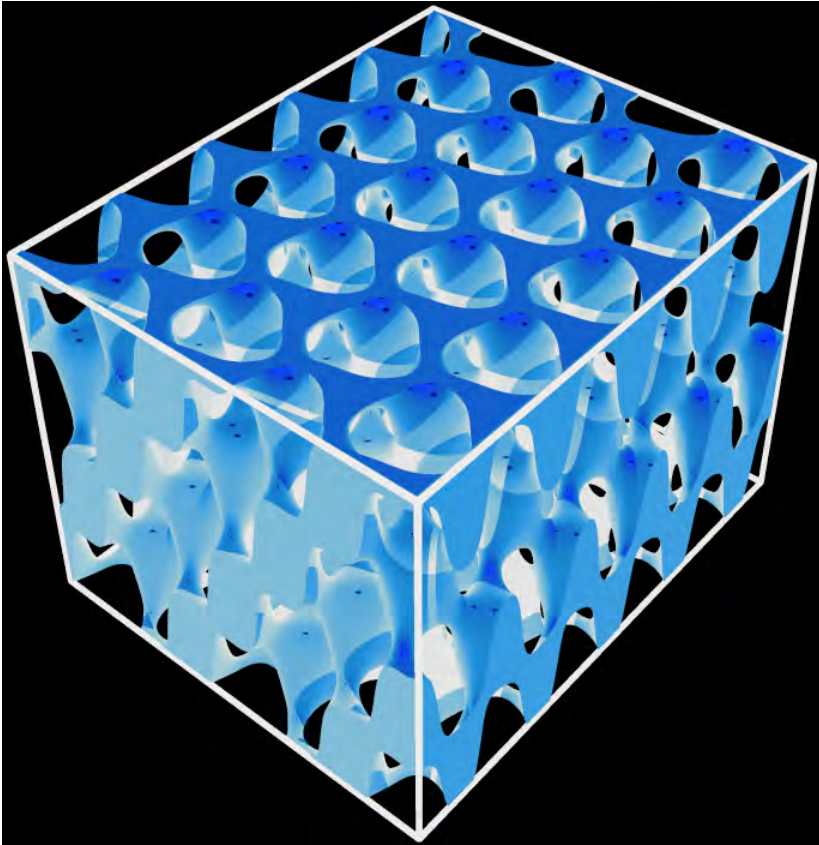
- ... is only valid in the limit  $\lambda / a \ll 1$ .
- ... neglects wave effects (diffraction, interference).
- ... treats light propagation in terms of rays.
- ... is employed, e.g., in raytracing programs.

## **“Normal” crystals ...**



- ... have lattice constants much smaller than the wavelength of light ( $\lambda / a \gg 1$ ).**
- ... can be treated as homogeneous media (Q.M.  $\rightarrow \epsilon, \mu, n, Z$ ).**
- ... are common optical materials.**
- ... have a refractive index  $n > 0$ .**

# Photonic crystals ...



- ... have lattice constants **comparable** to the wavelength of light ( $\lambda / a \approx 1$ ).
- ... are (in most cases) **artificial materials**.
- ... exhibit a **photonic band structure (Maxwell)**.
- ... can have a **complete photonic bandgap**.

# Metamaterials ...



- ... have lattice constants **smaller** than the wavelength of light ( $\lambda / a > 1$ ).
- ... are artificial materials.
- ... can be treated as homogeneous media (Maxwell  $\rightarrow \epsilon, \mu, n, Z$ ).
- ... can have a negative index of refraction  $n < 0$ .

# Photonics

**“Photonics is the science and technology of generating and controlling photons, particularly in the visible and near infra-red light spectrum.**

**The science of photonics includes the emission, transmission, amplification, detection, modulation, and switching of light. Photonic devices include optoelectronic devices such as lasers and photodetectors, as well as optical fibers, photonic crystals, planar waveguides and other passive optical elements.”**

# Example I

- **DWDM (Dense Wavelength Division Multiplexing)**



**Can we fabricate these devices on a micron scale?**

## **Example II**

- **Conventional optical fibers guide the light inside a glass core, thus showing dispersion. After a certain travel distance, information sent in the form of short laser pulses, smears out. Therefore, repeaters and amplifiers are needed.**

**Can we transmit light without dispersion?**

## **Example III**

- **With the further downscaling of conventional electronic components, quantum effects become important.**

**What can we expect from photonic structures on a wavelength or even smaller scales?**

## **Example IV**

- **All known natural materials exhibit a positive index of refraction.**

**Can we design and fabricate artificial materials with a negative index of refraction?**

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All of macroscopic electromagnetism can be described within the framework of the **macroscopic Maxwell equations:**

$$\vec{\nabla} \cdot \vec{D} = \rho$$

$$\vec{\nabla} \times \vec{E} = - \frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \times \vec{H} = \vec{j} + \frac{\partial \vec{D}}{\partial t}$$

with

$$\vec{D} = \epsilon_0 \vec{E} + \vec{P}$$

$$\vec{B} = \mu_0 \vec{H} + \vec{M}$$

$\vec{E}$  : electric field

$\vec{D}$  : dielectric displacement

$\vec{P}$  : polarization

$\rho$  : free charge density

$\vec{B}$  : magnetic induction

$\vec{H}$  : magnetic field

$\vec{M}$  : magnetization

$\vec{j}$  : free current density

The material properties enter via the **constitutive relations**.

For low light intensities, one usually finds a **linear relationship** between the polarization and the electric field as well as between the magnetization and magnetic field:

$$\vec{P}(t, \vec{r}) = \epsilon_0 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \vec{\chi}_e(t, t', \vec{r}, \vec{r}') \vec{E}(t', \vec{r}') dt' d\vec{r}'$$

$$\vec{M}(t, \vec{r}) = \mu_0 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \vec{\chi}_m(t, t', \vec{r}, \vec{r}') \vec{H}(t', \vec{r}') dt' d\vec{r}'$$



**Tensors!**

Here, we consider only **isotropic** materials with a **local response**:

$$\chi_e(t, t', \vec{r}, \vec{r}') = \chi_e(t, t') \delta(\vec{r} - \vec{r}')$$

$$\chi_m(t, t', \vec{r}, \vec{r}') = \chi_m(t, t') \delta(\vec{r} - \vec{r}')$$

The response functions must be **causal** and do not explicitly depend on time (**homogeneity in time**):

$$\chi_e(t, t') = \chi_e(t - t') \Theta(t - t')$$

$$\chi_m(t, t') = \chi_m(t - t') \Theta(t - t')$$

⇒

$$\vec{P}(t) = \epsilon_0 \int_{-\infty}^t \chi_e(t - t') \vec{E}(t') dt'$$

$$\vec{M}(t) = \mu_0 \int_{-\infty}^t \chi_m(t - t') \vec{H}(t') dt'$$

In the **frequency domain**, we get:

$$\vec{P}(t) = \epsilon_0 \int_{-\infty}^t \chi_e(t-t') \vec{E}(t') dt' \xrightarrow{\text{F.T.}} \vec{P}(\omega) = \epsilon_0 \chi_e(\omega) \vec{E}(\omega)$$

$$\vec{M}(t) = \mu_0 \int_{-\infty}^t \chi_m(t-t') \vec{H}(t') dt' \xrightarrow{\text{F.T.}} \vec{M}(\omega) = \epsilon_0 \chi_m(\omega) \vec{H}(\omega)$$

This finally leads to

$$\vec{D}(\omega) = \epsilon_0 (1 + \chi_e(\omega)) \vec{E}(\omega) = \epsilon_0 \epsilon(\omega) \vec{E}(\omega)$$

$$\vec{B}(\omega) = \mu_0 (1 + \chi_m(\omega)) \vec{H}(\omega) = \mu_0 \mu(\omega) \vec{H}(\omega)$$

**Electric permittivity**

**Magnetic permeability**

**Electromagnetic waves in homogenous media without dispersion, free charges and free currents ( $\epsilon = \text{const}$ ,  $\mu = \text{const}$ ,  $\rho = 0$ ,  $j = 0$ ):**

$$\vec{\nabla} \times \vec{E} = - \frac{\partial \vec{B}}{\partial t} \quad \xrightarrow[\frac{\partial}{\partial t}]{\vec{B} = \mu_0 \mu \vec{H}} \quad \frac{\partial}{\partial t} \vec{\nabla} \times \vec{E} = - \mu_0 \mu \frac{\partial^2}{\partial t^2} \vec{H}$$

$$\vec{\nabla} \times \vec{H} = \frac{\partial \vec{D}}{\partial t} \quad \xrightarrow[\vec{\nabla} \times]{\vec{D} = \epsilon_0 \epsilon \vec{E}} \quad \vec{\nabla} \times \vec{\nabla} \times \vec{H} = \epsilon_0 \epsilon \frac{\partial}{\partial t} \vec{\nabla} \times \vec{E}$$

**With  $\vec{\nabla} \times \vec{\nabla} \times = \vec{\nabla} (\vec{\nabla} \cdot) - \Delta$  and  $\vec{\nabla} \cdot \vec{B} = 0$  we obtain the **wave equation**:**

$$\Delta \vec{H}(t, \vec{r}) - \epsilon_0 \mu_0 \epsilon \mu \frac{\partial^2}{\partial t^2} \vec{H}(t, \vec{r}) = 0$$

**Electromagnetic waves in homogenous media without dispersion, free charges and free currents ( $\epsilon = \text{const}$ ,  $\mu = \text{const}$ ,  $\rho = 0$ ,  $j = 0$ ):**

$$\vec{\nabla} \times \vec{E} = - \frac{\partial \vec{B}}{\partial t} \quad \xrightarrow[\vec{\nabla} \times]{\vec{B} = \mu_0 \mu \vec{H}} \quad \vec{\nabla} \times \vec{\nabla} \times \vec{E} = - \mu_0 \mu \frac{\partial}{\partial t} \vec{\nabla} \times \vec{H}$$

$$\vec{\nabla} \times \vec{H} = \frac{\partial \vec{D}}{\partial t} \quad \xrightarrow[\partial / \partial t]{\vec{D} = \epsilon_0 \epsilon \vec{E}} \quad \frac{\partial}{\partial t} \vec{\nabla} \times \vec{H} = \epsilon_0 \epsilon \frac{\partial^2}{\partial t^2} \vec{E}$$

**With  $\vec{\nabla} \times \vec{\nabla} \times = \vec{\nabla} (\vec{\nabla} \cdot) - \Delta$  and  $\vec{\nabla} \cdot \vec{E} = 0$  we obtain the **wave equation**:**

$$\Delta \vec{E}(t, \vec{r}) - \epsilon_0 \mu_0 \epsilon \mu \frac{\partial^2}{\partial t^2} \vec{E}(t, \vec{r}) = 0$$

## With the complex ansatz for E and H ...

$$\vec{E}(t, \vec{r}) = \vec{E}_0 \exp[i(\vec{k} \cdot \vec{r} - \omega t)]$$

$$\vec{H}(t, \vec{r}) = \vec{H}_0 \exp[i(\vec{k} \cdot \vec{r} - \omega t)]$$

The **physical** electric and magnetic fields are obtained by taking the **real parts** of the complex quantities!

... we obtain from the wave equations:

$$k^2 = \varepsilon_0 \mu_0 \varepsilon \mu \omega^2$$

**Case 1: Plane waves**

$$\varepsilon \mu > 0 \Rightarrow k_i \in \mathfrak{R}, i \in \{x, y, z\}$$

**Case 2: Evanescent modes**

$$\varepsilon \mu < 0 \Rightarrow k_i \in \mathfrak{I}, i \in \{x, y, z\}$$

## Plane waves ...

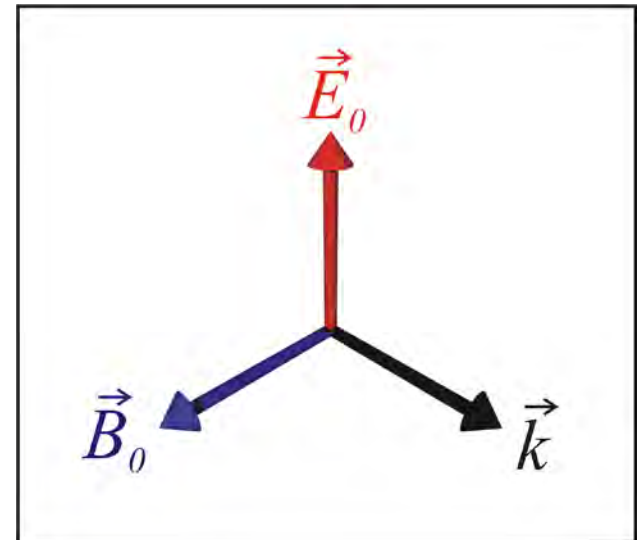
$$\vec{E}(t, \vec{r}) = \vec{E}_0 \exp[i(\vec{k} \cdot \vec{r} - \omega t)]$$

$$\vec{B}(t, \vec{r}) = \vec{B}_0 \exp[i(\vec{k} \cdot \vec{r} - \omega t)]$$

... are transversal:

$$\vec{\nabla} \times \vec{E} = \begin{pmatrix} ik_y E_z - ik_z E_y \\ ik_x E_z - ik_z E_x \\ ik_x E_y - ik_y E_x \end{pmatrix} = i\vec{k} \times \vec{E} \stackrel{!}{=} -i\omega \vec{B}$$

$$\vec{\nabla} \cdot \vec{B} = i(k_x B_x + k_y B_y + k_z B_z) = i\vec{k} \cdot \vec{B} \stackrel{!}{=} 0$$



Moreover,  $E$  and  $B$  are in phase.

**The planes of constant phase propagate with the phase velocity  $c$  :**

$$c^2 = \frac{\omega^2}{k^2} = \frac{1}{\epsilon_0 \epsilon \mu_0 \mu} = \frac{c_0^2}{\epsilon \mu} = \frac{c_0^2}{n^2}$$

**The material properties enter via the refractive index ...**

$$n^2 = \epsilon \mu \Rightarrow n = \pm \sqrt{\epsilon \mu} \longrightarrow$$

$$\text{Dielectric materials: } n = \sqrt{\epsilon \mu} \\ (\epsilon, \mu > 0)$$

**... and the impedance**

$$Z = \sqrt{\frac{\mu_0 \mu}{\epsilon_0 \epsilon}} \quad Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} \approx 376.7 \Omega$$

**The energy density  $w$  of an electromagnetic wave in a nondispersive medium is given by**

$$w = \frac{1}{4} \Re \left( \vec{E}_0 \cdot \vec{D}_0^* + \vec{H}_0 \cdot \vec{B}_0^* \right) \leftarrow \text{This formula is valid only for nondispersive media!}$$

**The corresponding time averaged energy flux density is given by the Poynting vector**

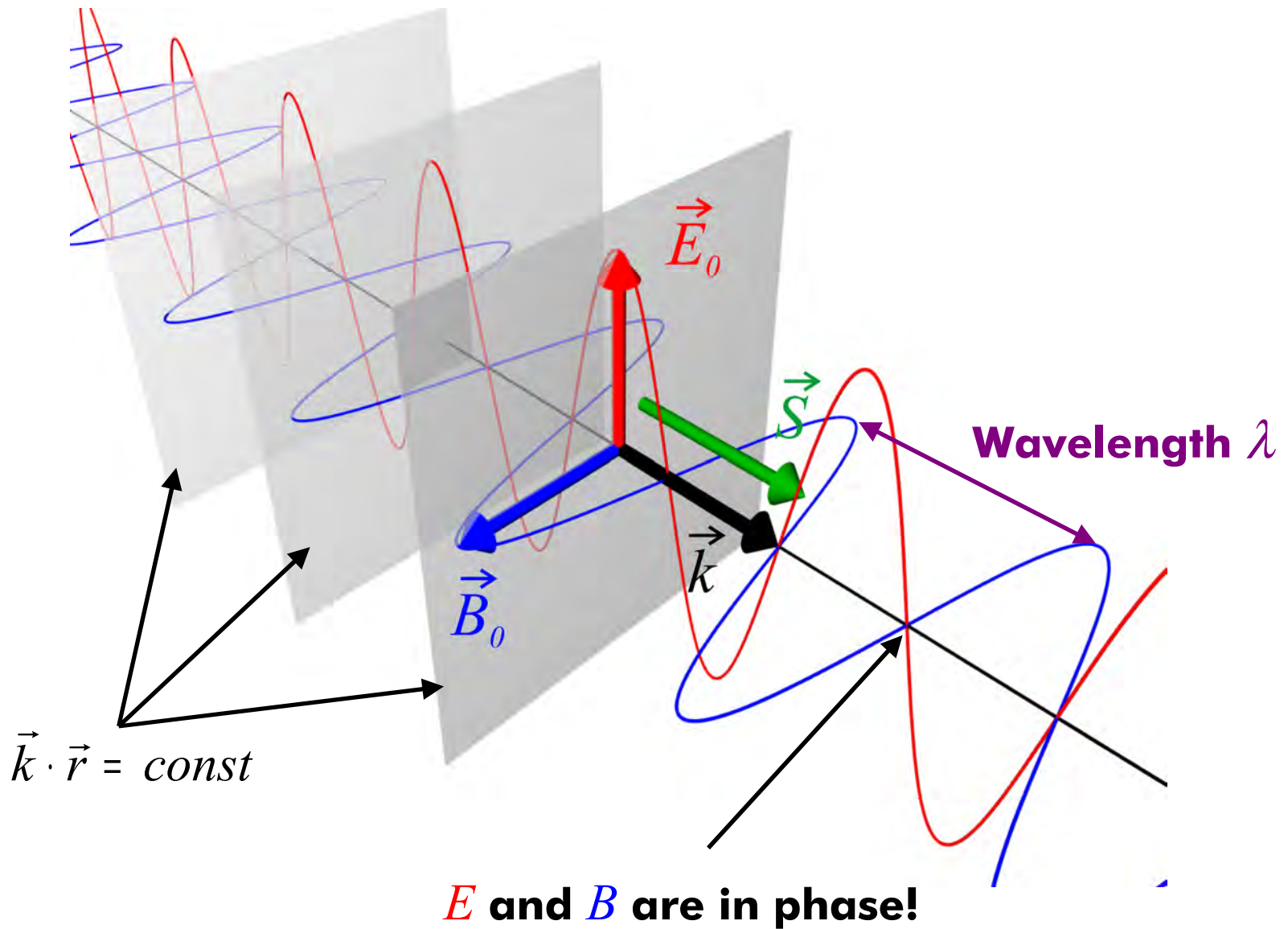
$$\vec{S} = \frac{1}{2} \Re \left( \vec{E}_0 \times \vec{H}_0^* \right) \leftarrow \mu > 0 \Rightarrow \vec{S} \parallel \vec{k}$$

**The magnitude of  $\vec{S}$  denotes the intensity of the electromagnetic field:**

$$I = |\vec{S}| = \frac{1}{2} \epsilon_0 \epsilon c |\vec{E}_0|^2$$

**These quantities are spatially constant for plane waves.**

## Plane waves ...

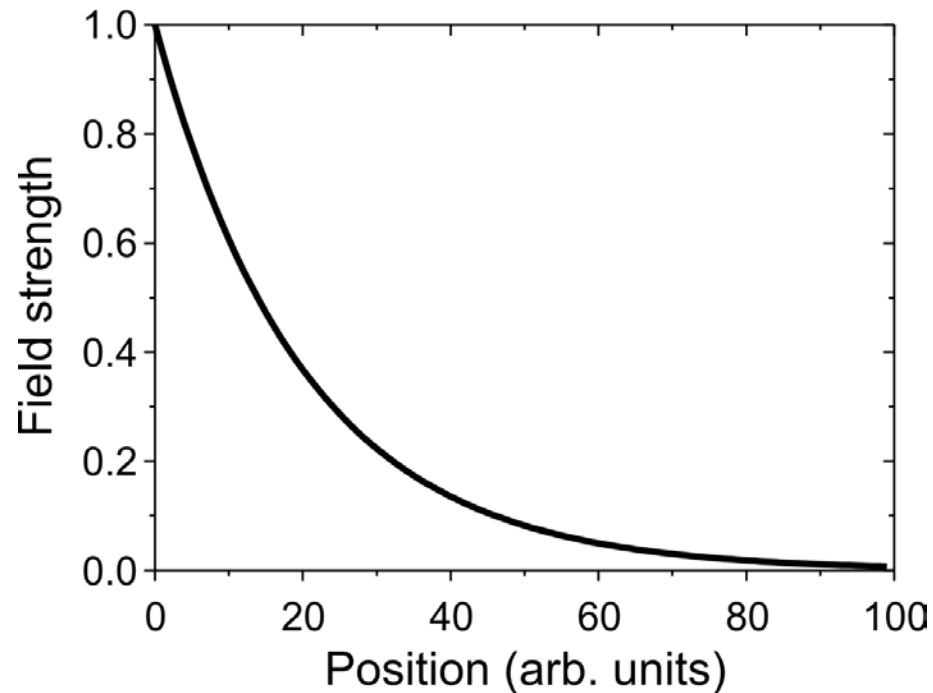


## Evanescent modes ...

$$\vec{E}(t, \vec{r}) = \vec{E}_0 \exp[-|\vec{k}| \vec{e}_k \cdot \vec{r}] \exp[-i\omega t]$$

$$\vec{B}(t, \vec{r}) = \vec{B}_0 \exp[-|\vec{k}| \vec{e}_k \cdot \vec{r}] \exp[-i\omega t]$$

**... exhibit exponentially decaying field strengths (E and B).**



## Evanescent modes ...

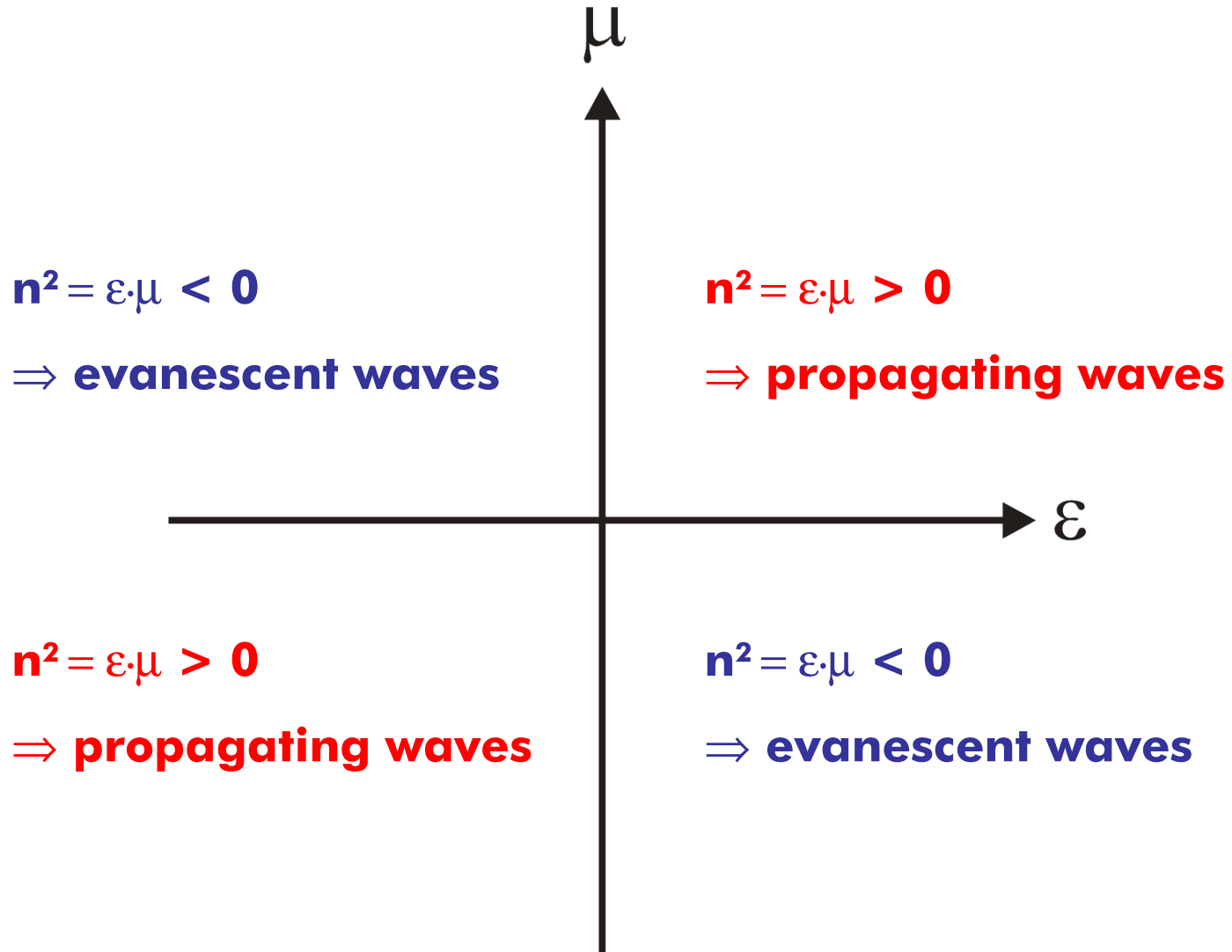
**... do not transport energy since the time-averaged normal component of the Poynting vector vanishes :**

$$\vec{S}_{\vec{e}_k} = \frac{1}{2} \Re \left( \vec{e}_k \cdot \left[ \vec{E}_0 \times \vec{H}_0^* \right] \right) = \frac{1}{2\omega \mu_0 \mu} \Re \left( \vec{e}_k \cdot \underbrace{\left[ \vec{E}_0 \times (\vec{k} \times \vec{E}_0)^* \right]}_{\text{Purely imaginary!}} \right) = 0$$

**Purely imaginary!**

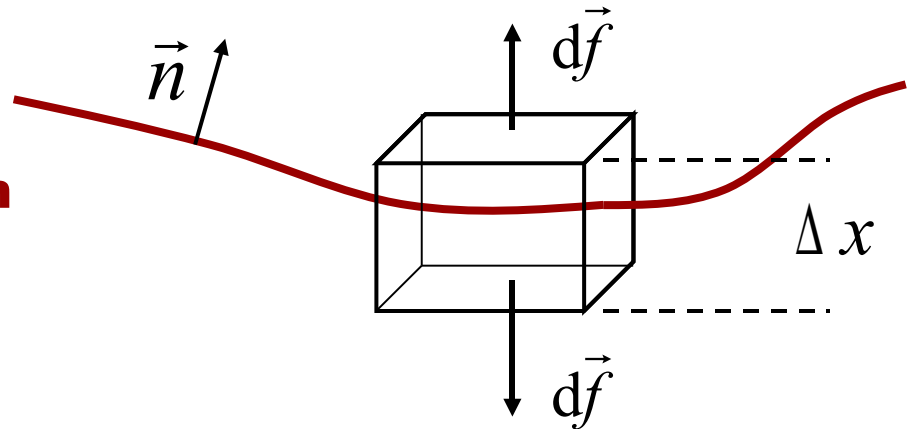
**Therefore, evanescent modes do only have a noticeable field strength at interfaces.**

# Classification of electromagnetic modes



# Electromagnetic fields at interfaces

- Use 3<sup>rd</sup> Maxwell equation
- Use Gauss-Theorem

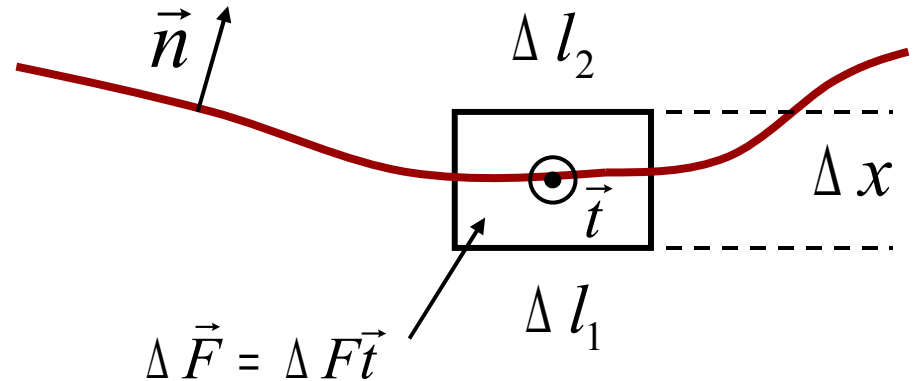


$$0 = \int_{\Delta V} d^3 r \vec{\nabla} \cdot \vec{B} = \int_{S(\Delta V)} d\vec{f} \cdot \vec{B} \xrightarrow{\Delta x \rightarrow 0} |d\vec{f}| \vec{n} \cdot (\vec{B}_2 - \vec{B}_1)$$

⇒ **Normal component of B must be continuous**

# Electromagnetic fields at interfaces

- Use 4<sup>th</sup> Maxwell equation
- Use Stokes-Theorem



$$\left. \begin{aligned} \int_{\Delta F} d\vec{f} \cdot \vec{\nabla} \times \vec{H} &= \int_{\Delta F} d\vec{f} \cdot \vec{j}_f + \frac{\partial}{\partial t} \int_{\Delta F} d\vec{f} \cdot \vec{D} - \xrightarrow{\Delta x \rightarrow 0} \Delta l (\vec{j}_F \cdot \vec{t}) \\ \int_{\Delta F} d\vec{f} \cdot \text{rot } \vec{H} &= \int_{\partial \Delta F} d\vec{s} \cdot \vec{H} - \xrightarrow{\Delta x \rightarrow 0} \Delta l (\vec{t} \times \vec{n}) \cdot (\vec{H}_2 - \vec{H}_1) \end{aligned} \right\} \begin{aligned} &(\vec{t} \times \vec{n}) \cdot (\vec{H}_2 - \vec{H}_1) \\ &= \vec{j}_F \cdot \vec{t} \end{aligned}$$

$\Rightarrow$  (no surface current) Tangential component of H must be continuous

# Electromagnetic fields at interfaces

With a similar derivation for **E** and **D** follows:

- **D** normal
- **E** tangential
- **B** normal
- **H** tangential

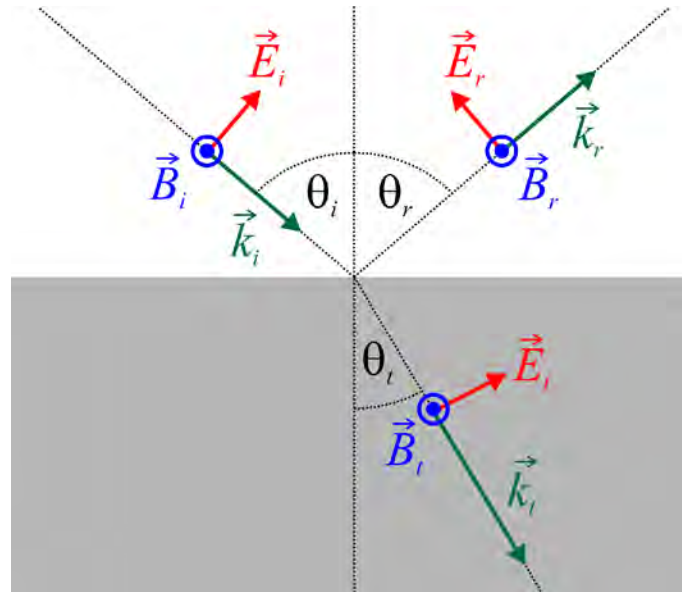
have to be continuous across charge- and current-free interfaces.

We obtain for the other field components:

$$D_{2t} = \frac{\epsilon_2}{\epsilon_1} D_{1t} \quad E_{2n} = \frac{\epsilon_1}{\epsilon_2} E_{1n} \quad B_{2t} = \frac{\mu_2}{\mu_1} B_{1t} \quad H_{2n} = \frac{\mu_1}{\mu_2} H_{1n}$$

# Refraction at an interface – Fresnel formulas

**p-polarization**



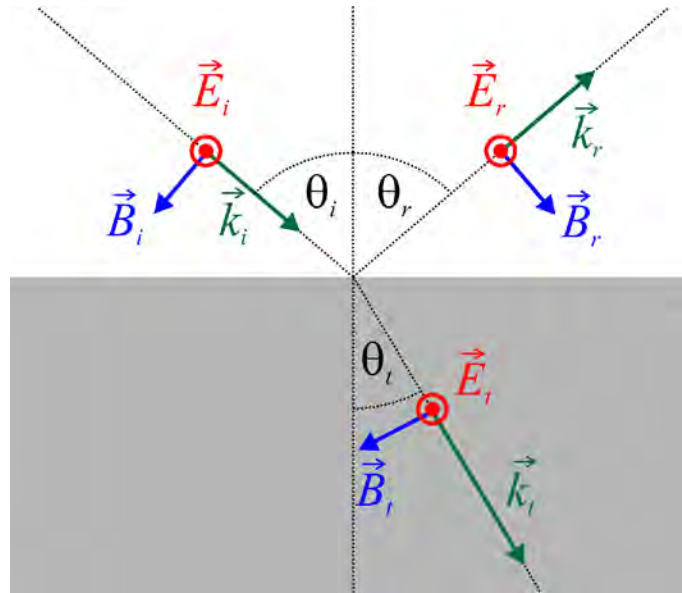
$$\theta_i = \theta_r \quad n_i \sin(\theta_i) = n_t \sin(\theta_t)$$

$$r_p = \left( \frac{E_r}{E_i} \right)_p = \frac{(n_t / \mu_t) \cos(\theta_i) - (n_i / \mu_i) \cos(\theta_t)}{(n_i / \mu_i) \cos(\theta_t) + (n_t / \mu_t) \cos(\theta_i)}$$

$$t_p = \left( \frac{E_t}{E_i} \right)_p = \frac{2(n_i / \mu_i) \cos(\theta_i)}{(n_i / \mu_i) \cos(\theta_t) + (n_t / \mu_t) \cos(\theta_i)}$$

# Refraction at an interface – Fresnel formulas

**s-polarization**

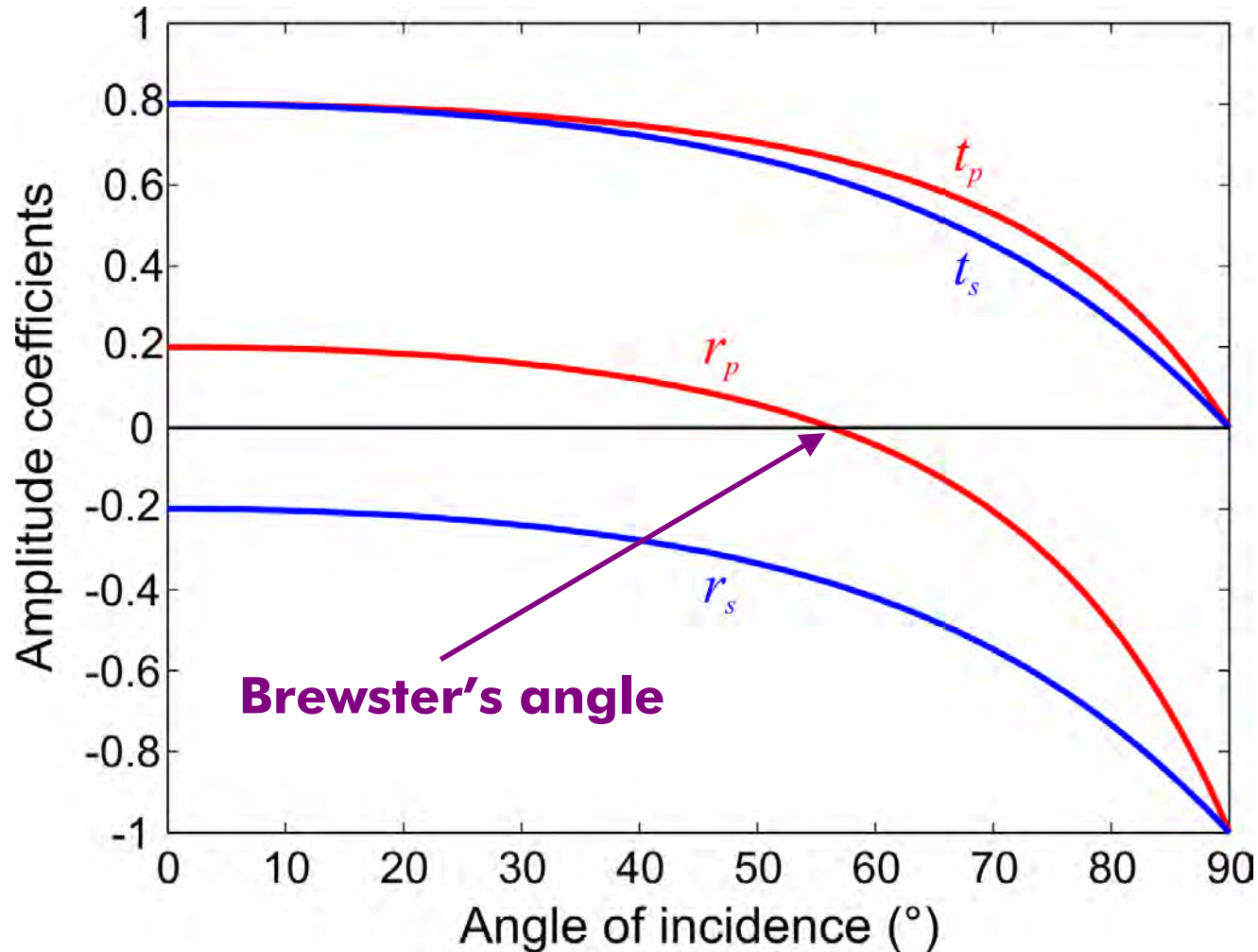


$$\theta_i = \theta_r \quad n_i \sin(\theta_i) = n_t \sin(\theta_t)$$

$$r_s = \left( \frac{E_r}{E_i} \right)_s = \frac{(n_i / \mu_i) \cos(\theta_i) - (n_t / \mu_t) \cos(\theta_t)}{(n_i / \mu_i) \cos(\theta_i) + (n_t / \mu_t) \cos(\theta_t)}$$

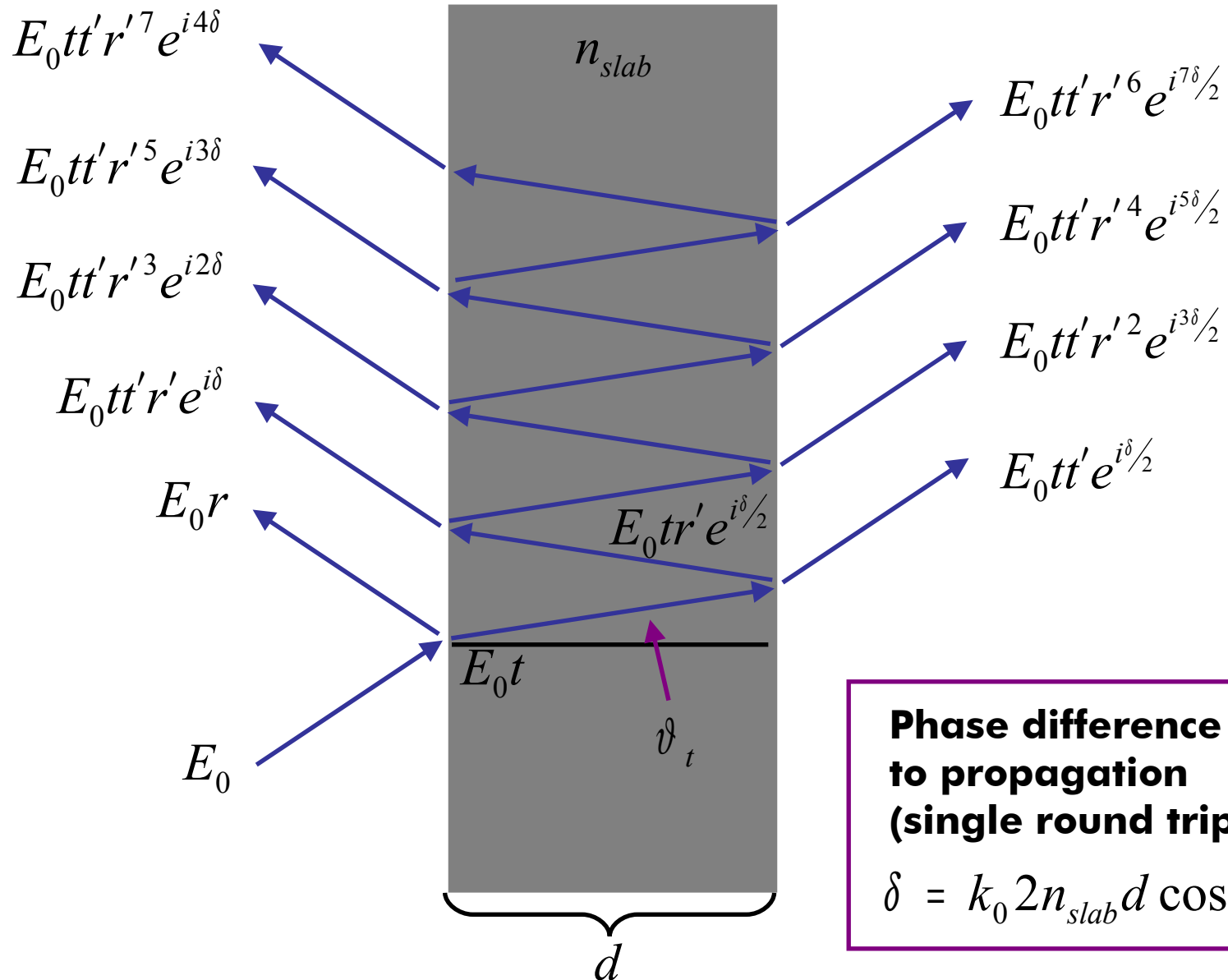
$$t_s = \left( \frac{E_t}{E_i} \right)_s = \frac{2(n_i / \mu_i) \cos(\theta_i)}{(n_i / \mu_i) \cos(\theta_i) + (n_t / \mu_t) \cos(\theta_t)}$$

# Refraction at an interface – Fresnel formulas



**Parameters:**  $\epsilon_1=1.0$ ,  $\mu_1=1.0$ ,  $\epsilon_2=2.25$ ,  $\mu_2=1.0$

# A slab of matter: Fabry-Perot modes



**Phase difference due to propagation (single round trip):**

$$\delta = k_0 2n_{slab} d \cos(\vartheta_t)$$

# A slab of matter: Fabry-Perot modes

**The total transmitted electric field is given by the superposition of all partially transmitted electric fields:**

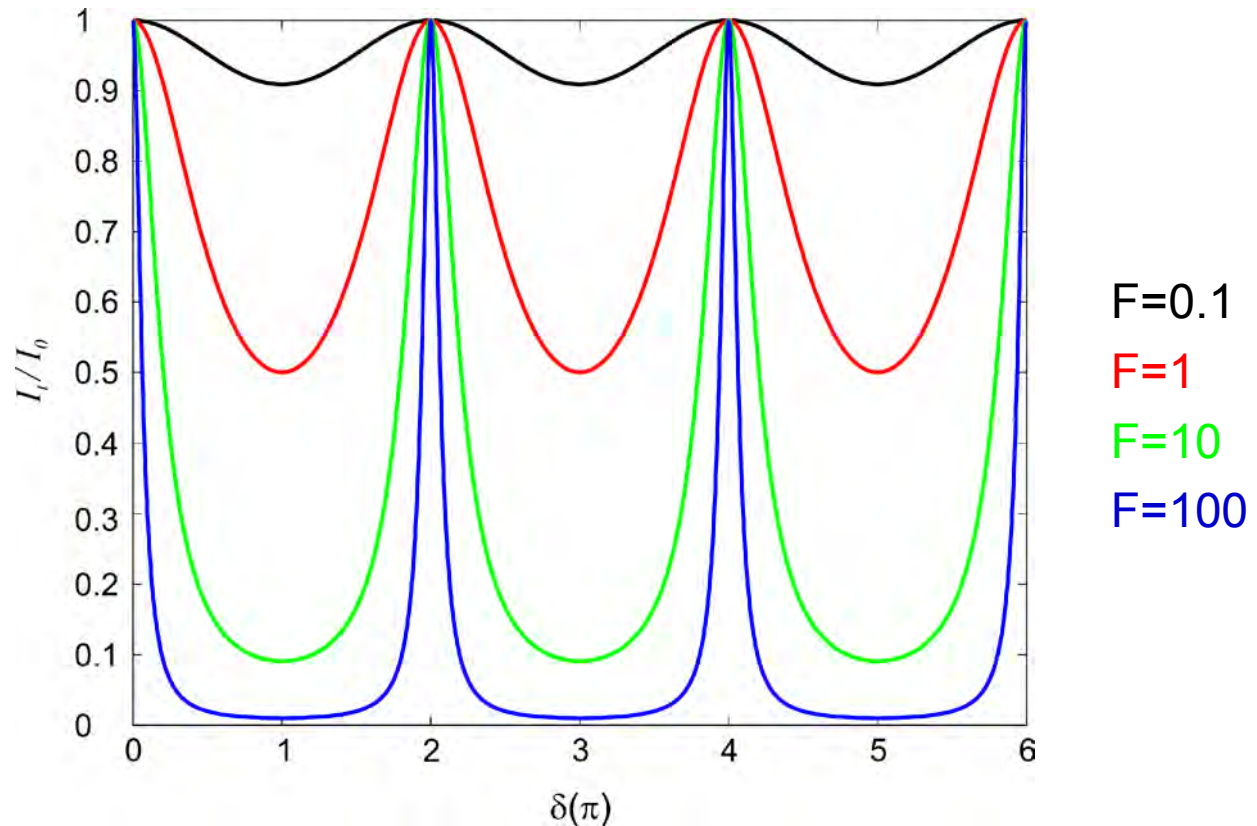
$$E_t = E_0 t t' e^{i\delta/2} + E_0 t t' r'^2 e^{i3\delta/2} + E_0 t t' r'^4 e^{i5\delta/2} + E_0 t t' r'^6 e^{i7\delta/2} + \dots$$

**After a little bit of algebra we obtain the intensity of the total transmitted electromagnetic field (for lossless media)**

$$I_t = I_0 \frac{1}{1 + F \sin^2(\delta / 2)}$$

**with the finesse factor**  $F = \left( \frac{2r}{1 - r^2} \right)^2$

# A slab of matter: Fabry-Perot modes



**The transmittance is maximal for  $\delta = 2m\pi$ ,  $m \in \{0, 1, 2, \dots\}$**   
**since all partial waves are in phase:**

$$E_t = E_0 t t' e^{i\delta/2} (1 + r'^2 + r'^4 + r'^6 + \dots)$$

# A slab of matter: Fabry-Perot modes

**The total reflected electric field is given by the superposition of all partially reflected electric fields:**

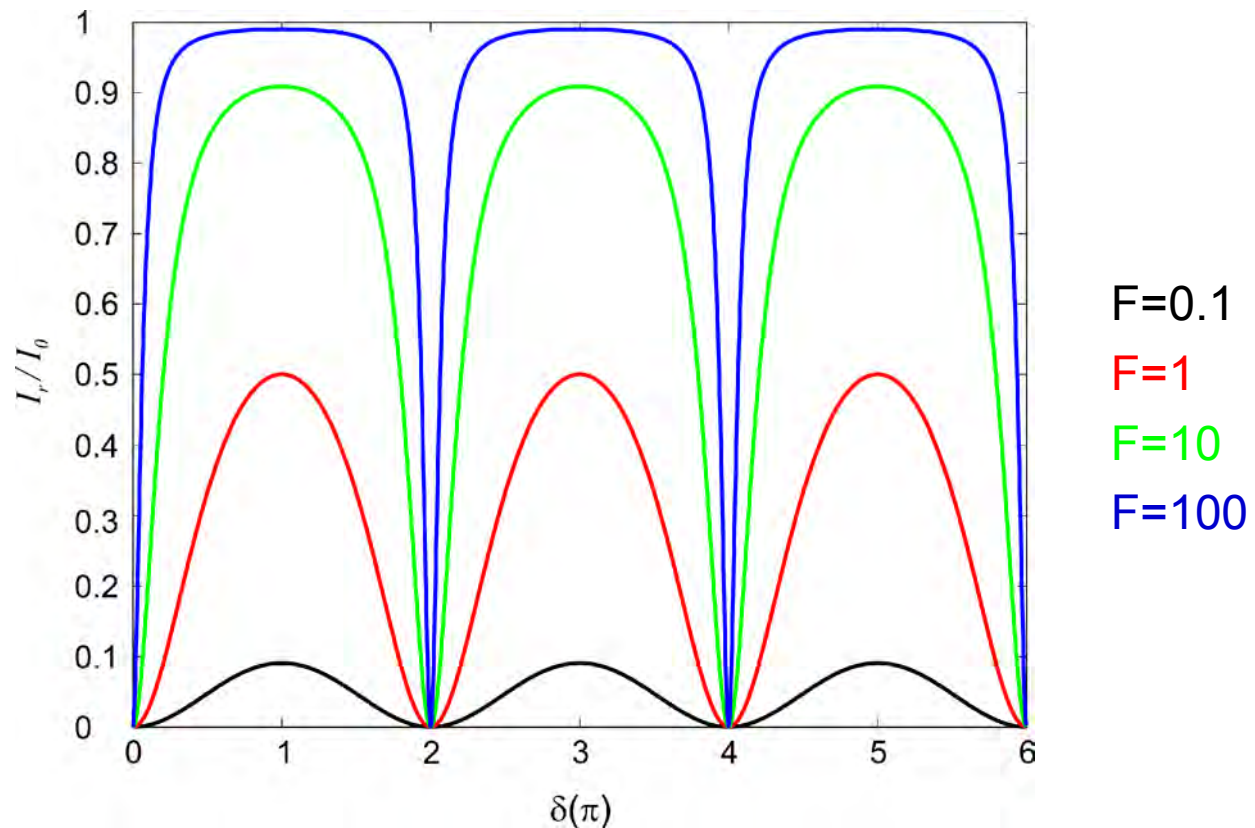
$$E_r = E_0 r + E_0 t t' r' e^{i\delta} + E_0 t t' r'^3 e^{i2\delta} + E_0 t t' r'^5 e^{i3\delta} + \dots$$

**After a little bit of algebra we obtain the intensity of the total reflected electromagnetic field (for lossless media)**

$$I_r = I_0 \frac{F \sin^2(\delta / 2)}{1 + F \sin^2(\delta / 2)}$$

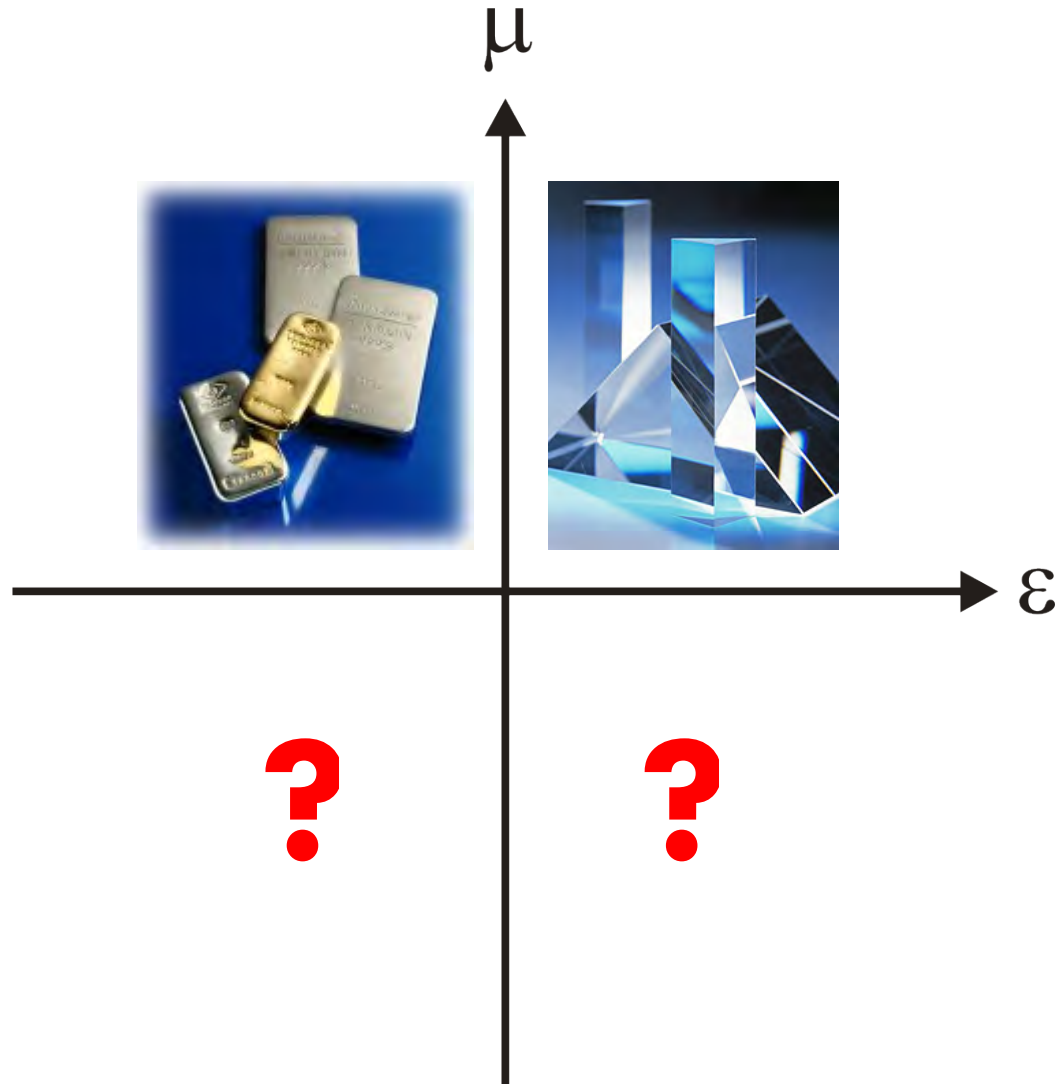
**with the finesse factor**  $F = \left( \frac{2r}{1 - r^2} \right)^2$

# A slab of matter: Fabry-Perot modes

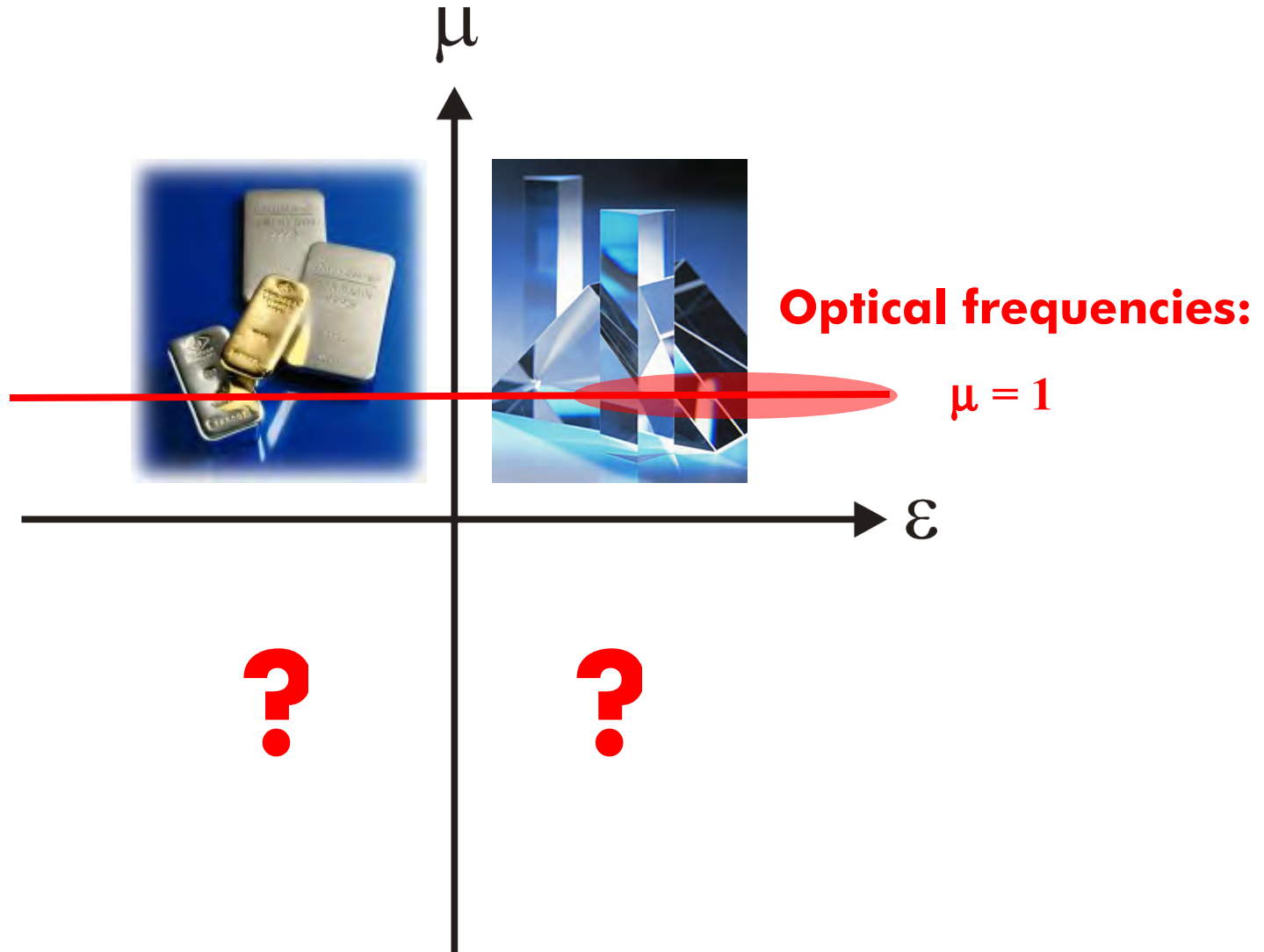


**The reflectance is maximal for  $\delta = (2m + 1)\pi$ ,  $m \in \{0, 1, 2, \dots\}$**

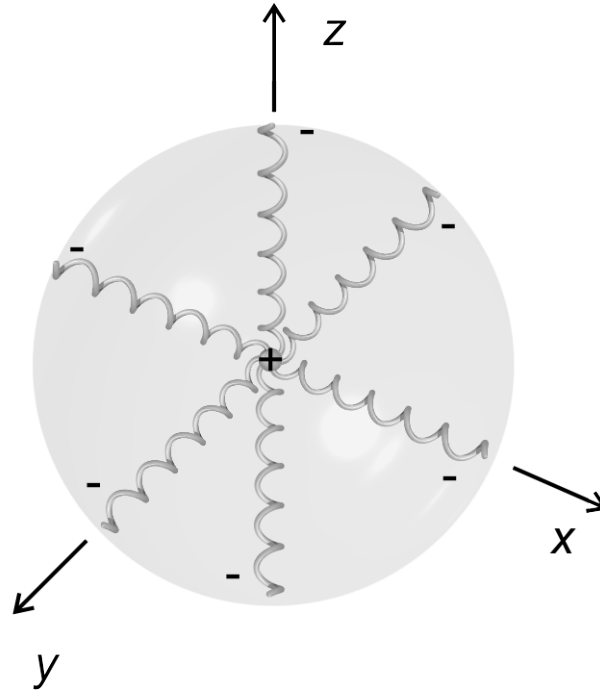
# Classification of optical materials



# Classification of optical materials



# Lorentz Oscillator modell



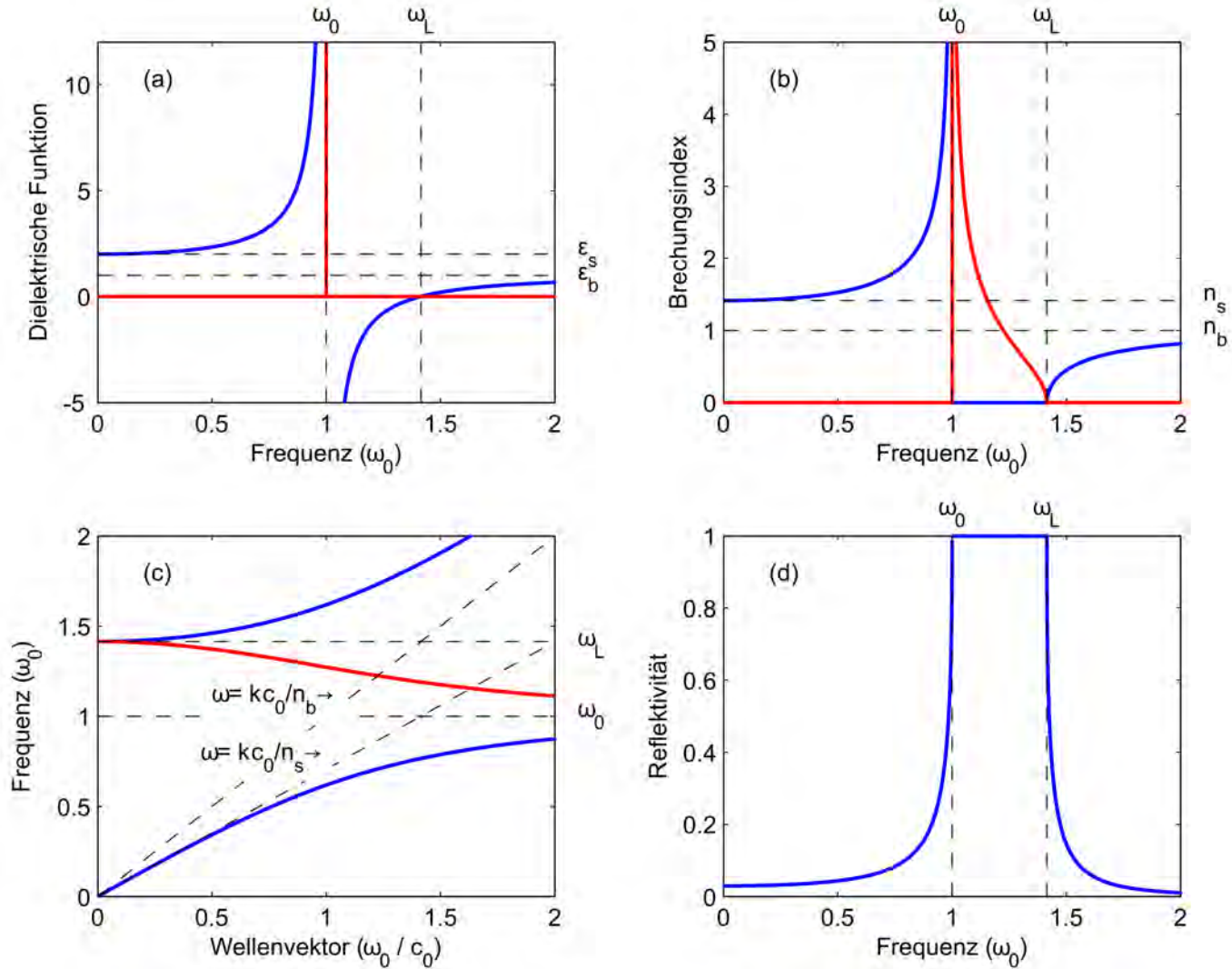
**Equation of motion:**

$$m \frac{d^2 x}{dt^2} + m \gamma_0 \frac{dx}{dt} + m \omega_0^2 x = -q E_0 e^{-i \omega t}$$

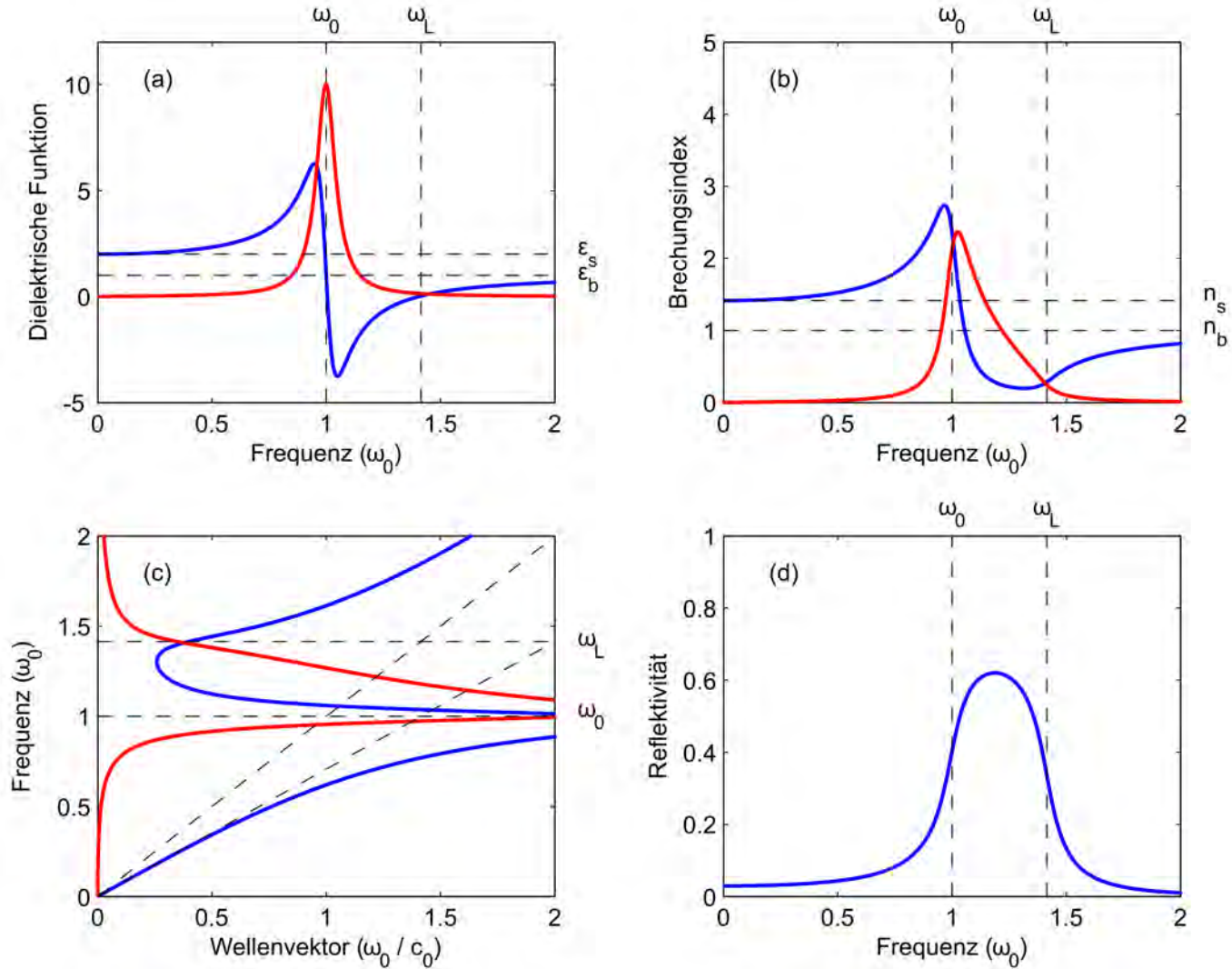
**Lorentz dielectric function:**

$$\epsilon(\omega) = 1 + \frac{Nq^2}{m\epsilon_0} \frac{1}{\omega_0^2 - \omega^2 - i\omega\gamma_0}$$

# Lorentz Oscillator modell – without losses



# Lorentz Oscillator modell – with losses



## 0. Introduction

### 1. Reminder:

E-Dynamics in homogenous media and at interfaces

## 2. Photonic Crystals

### 2.1 Introduction

### 2.2 1D Photonic Crystals

### 2.3 2D and 3D Photonic Crystals

### 2.4 Numerical Methods

### 2.5 Fabrication

### 2.6 Non-linear optics and Photonic Crystals

### 2.7 Quantumoptics

### 2.8 Chiral Photonic Crystals

### 2.9 Quasicrystals

### 2.10 Photonic Crystal Fibers – „Holey“ Fibers

## 3. Metamaterials and Plasmonics

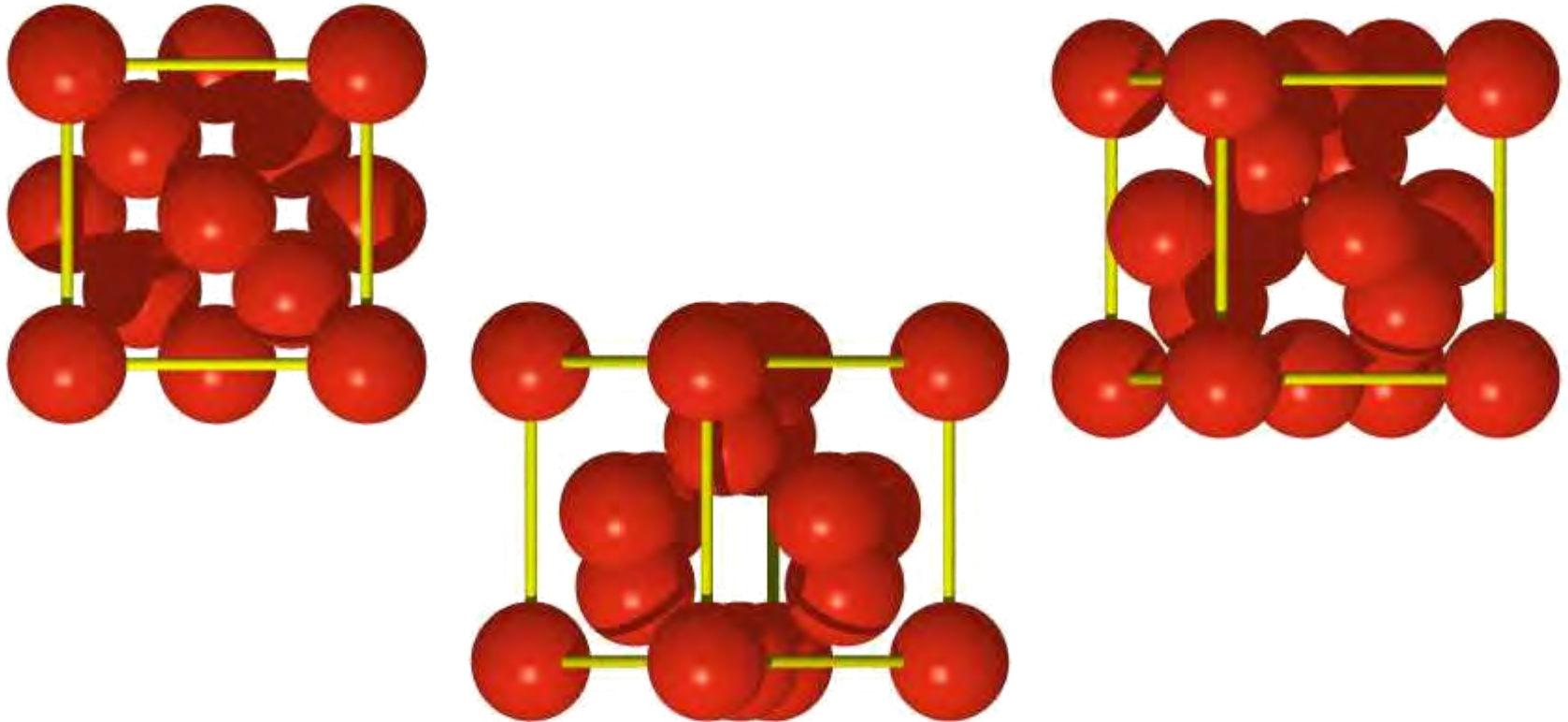
### 3.1 Introduction

### 3.2 Background

### 3.2 Fabrication

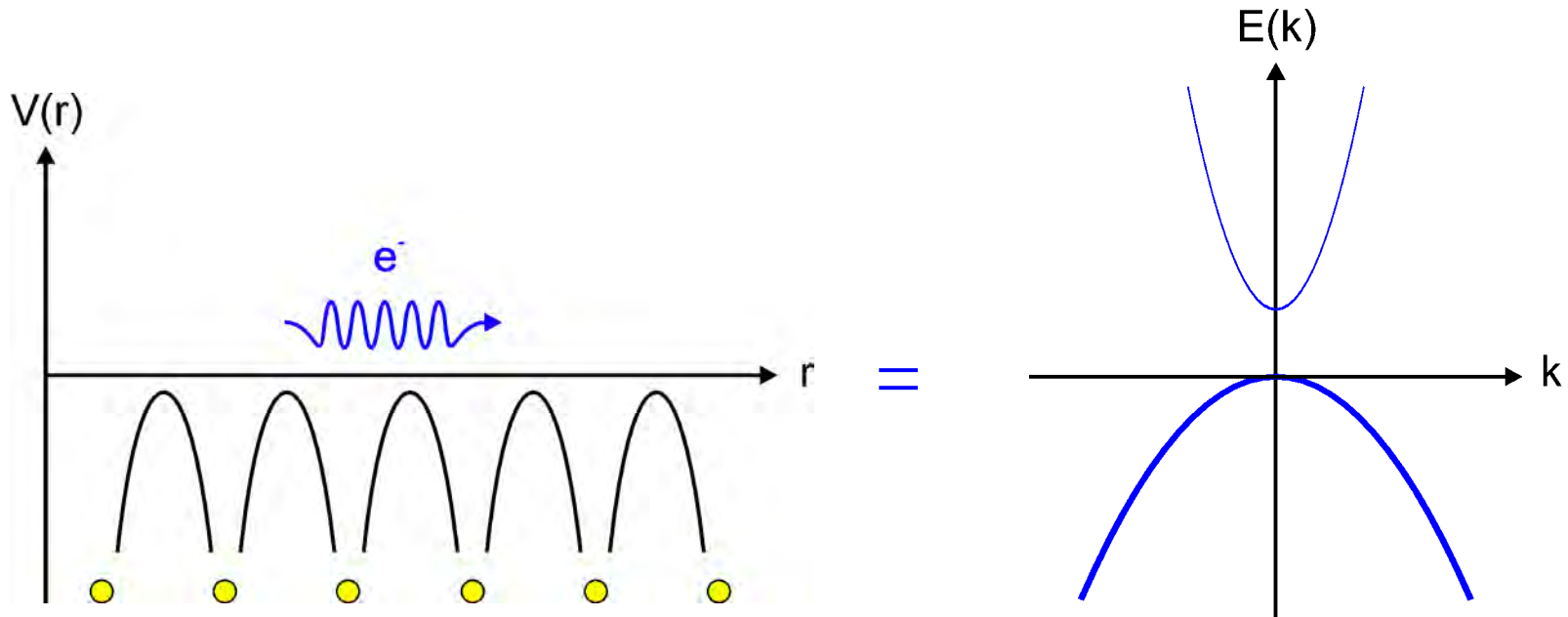
### 3.3 Experiments

# Silicon, a semiconductor crystal



Is there such a thing as a “semiconductor for light” ?

# Semiconductors

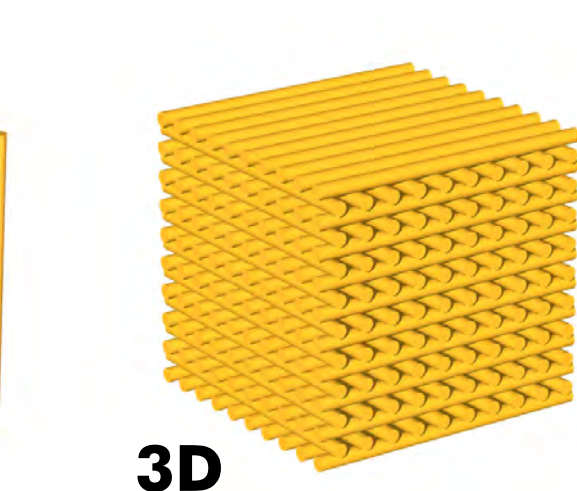
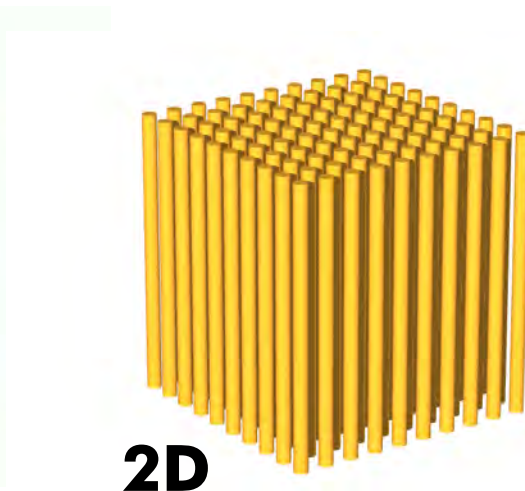
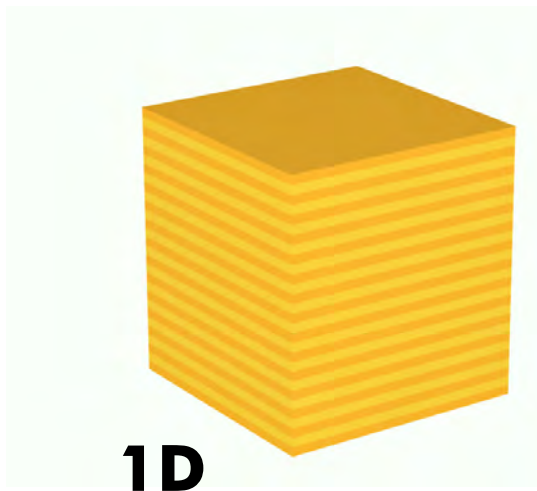


**Periodic potential for electrons**

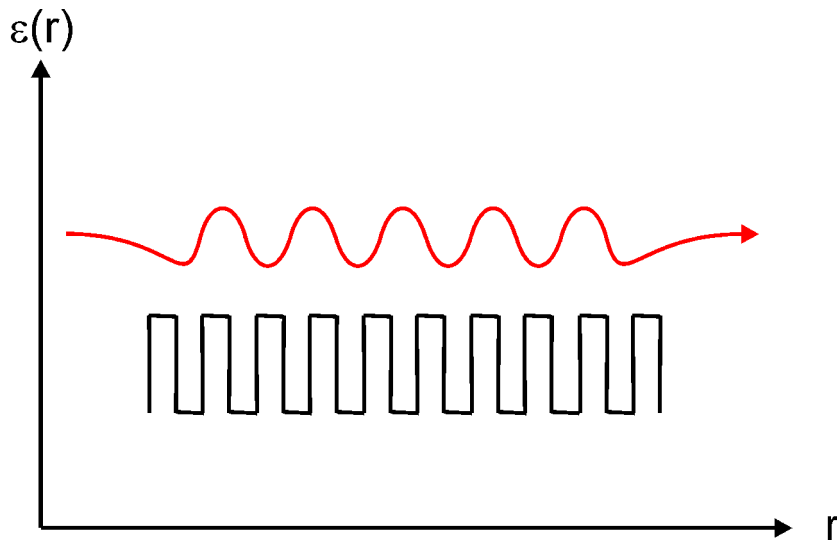
**Band structure for electrons**

# Photonic Crystals

- **Dielectric or metallic materials with a dielectric function  $\vec{\epsilon}(\vec{r}, \omega)$  that is periodically modulated along at least one spatial direction:**

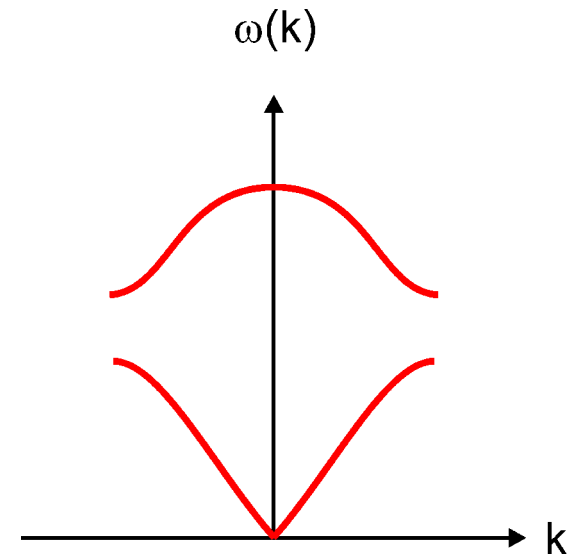


# Photonic Crystals



**Periodic "potential" for photons**

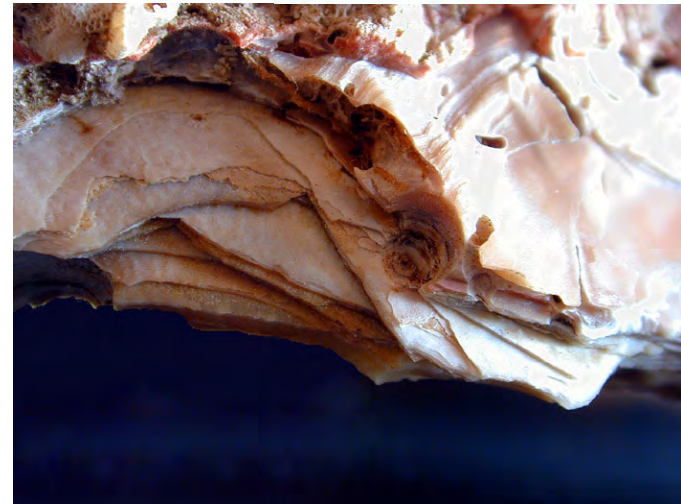
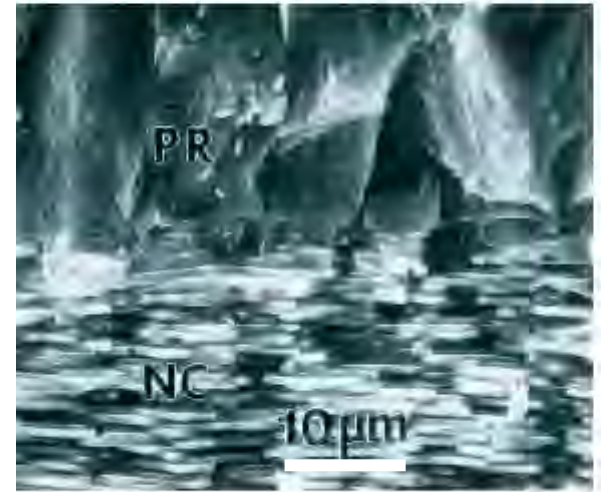
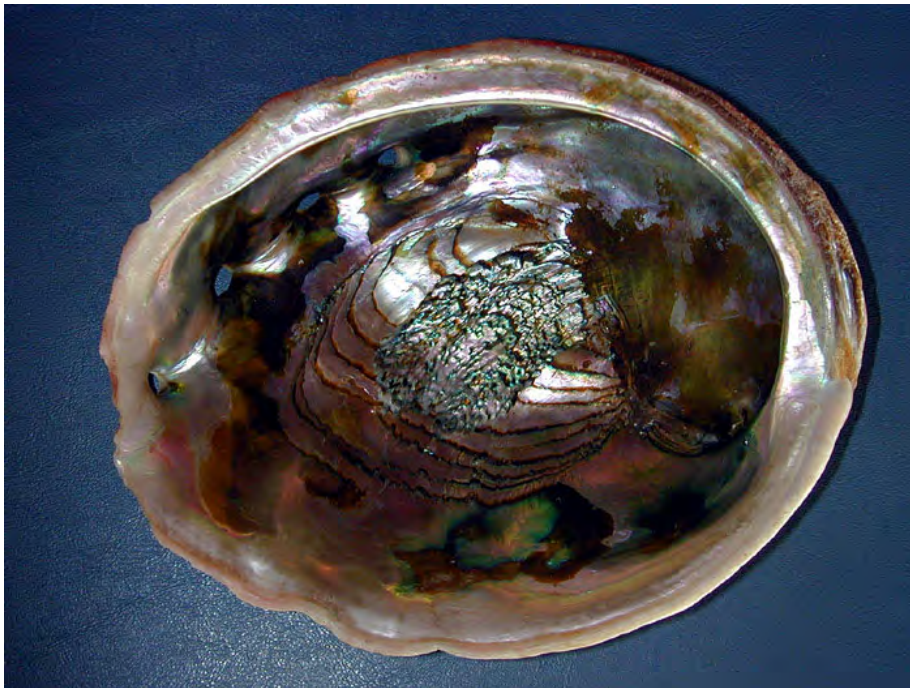
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**Band structure for photons**

# 1D Photonic Crystals in nature

- **Mother-of-pearl**



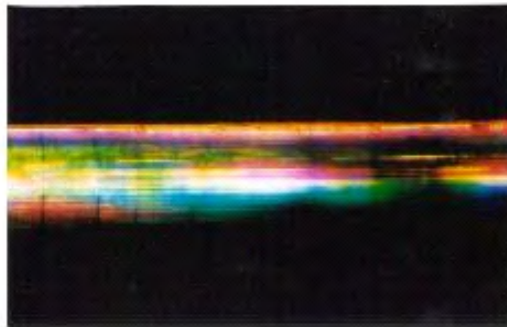
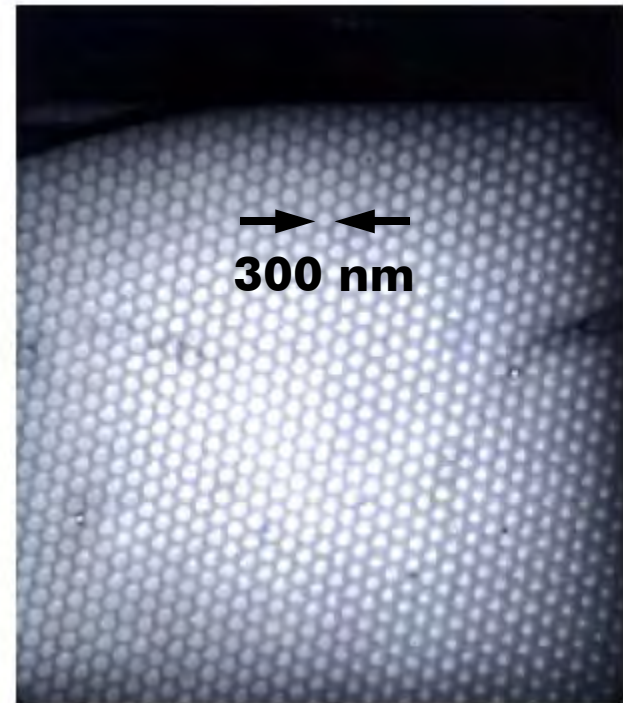
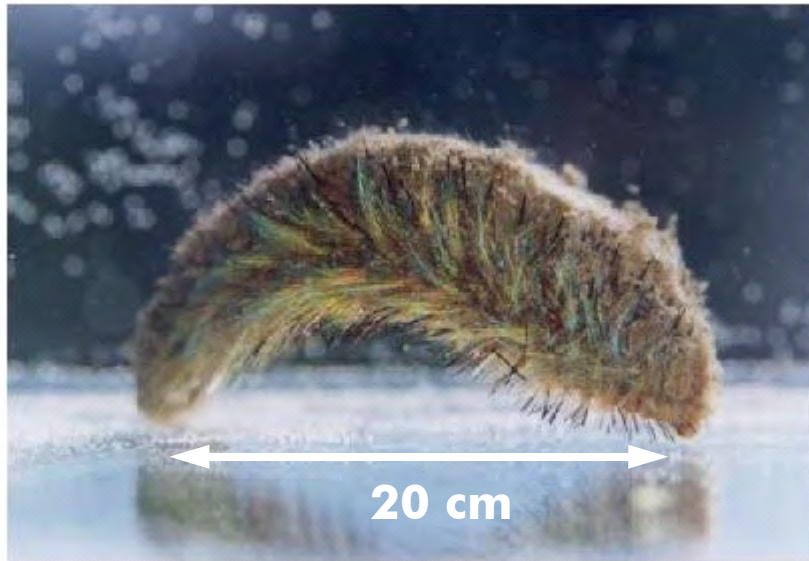
**Aragonite [CaCO<sub>3</sub>] / protein layers**

taken from:

<http://www.biosbcc.net/ocean/marinesci/06future/abrepro.htm>

<http://www.solids.bnl.gov/~dimasi/bones/abalone/>

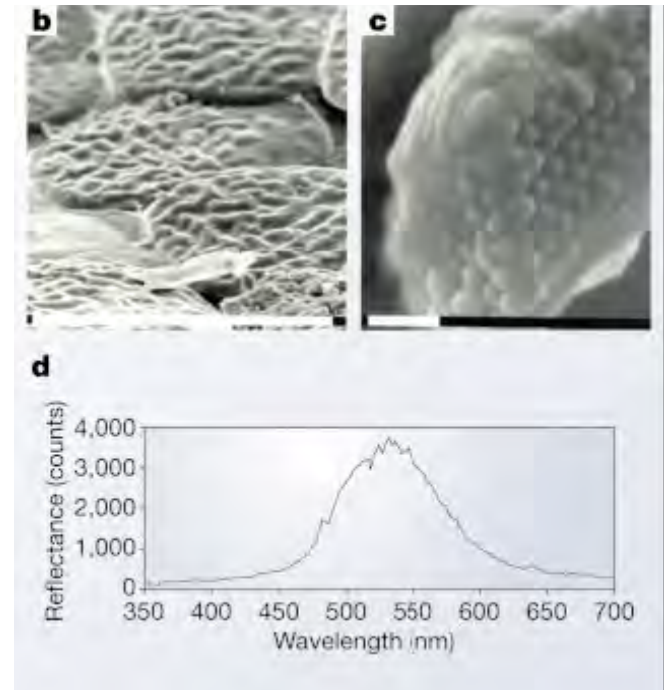
# 2D Photonic Crystals in nature



**Sea-mouse**

# 3D Photonic Crystals in nature

- **Pachyrhynchus argus**

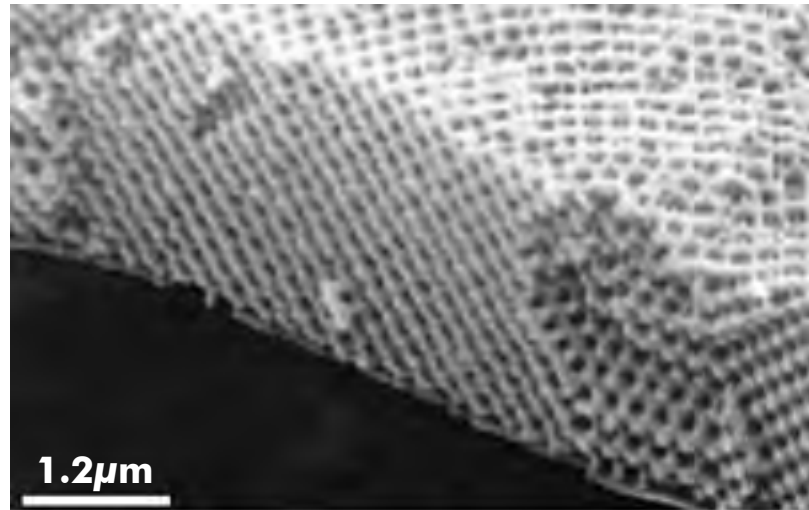


Taken from:

• <http://www.shgresources.com/nv/symbols/gemstoneep>

• A. R. Parker et al., Nature 426, 786 (2003)

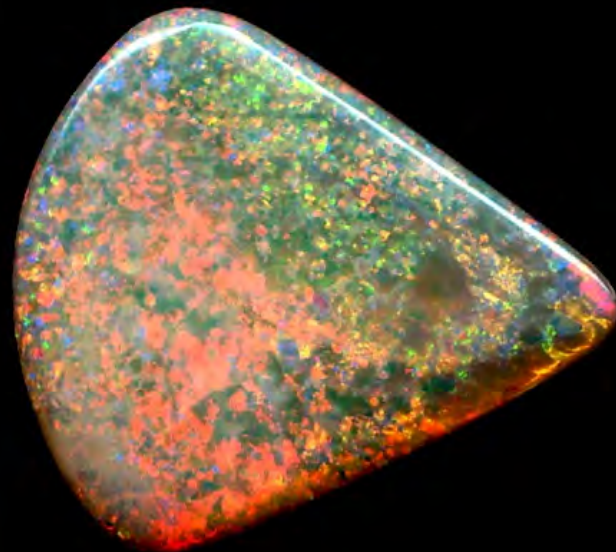
# 3D Photonic Crystals in nature



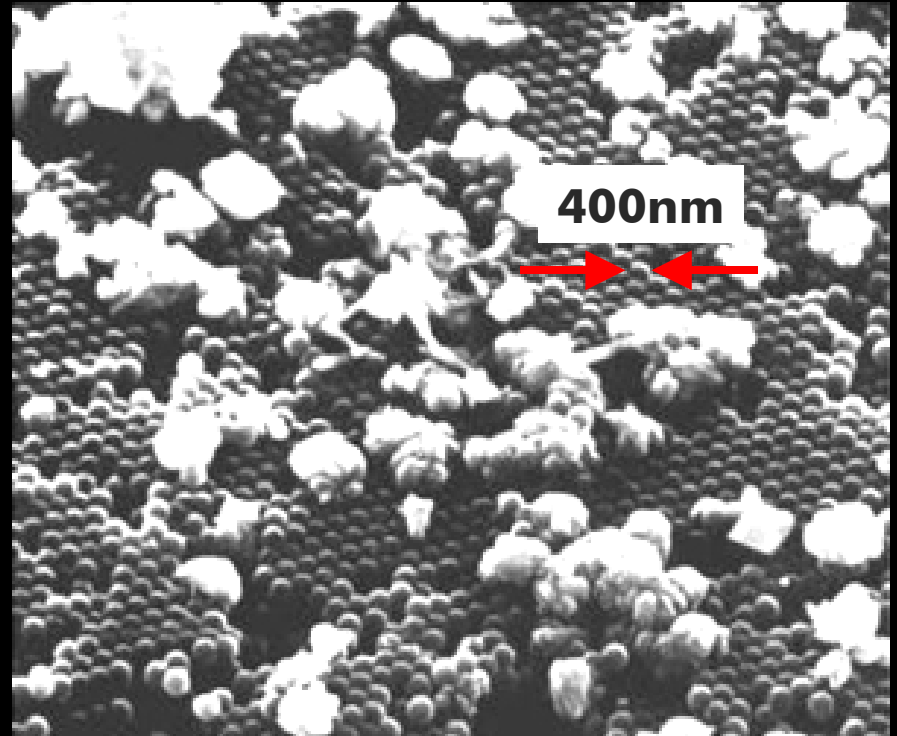
**Morpho Rhetenor und Parides Sesostris**



# Opals: 3D Photonic Crystals



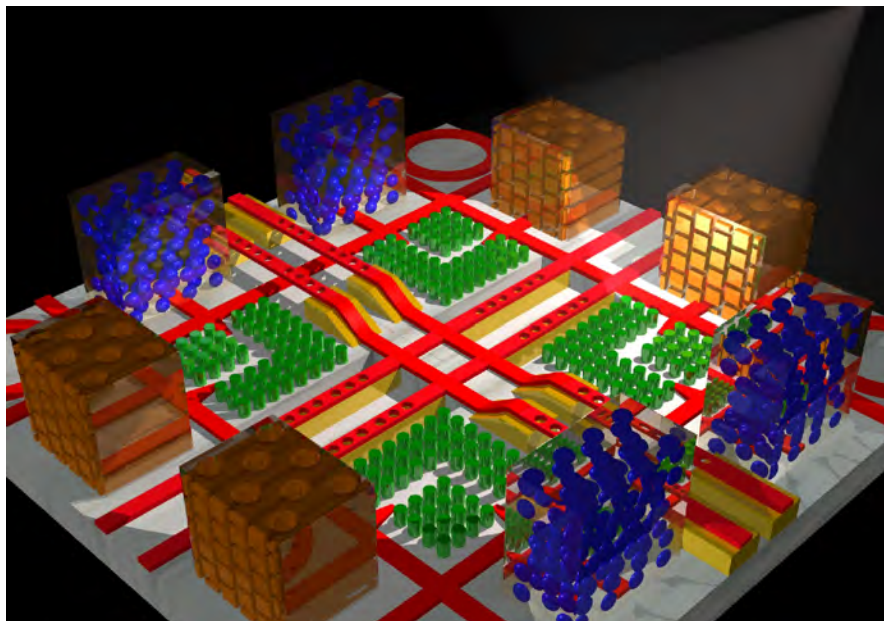
# A closer look at an Opal



# **Visions for Photonic Crystals**

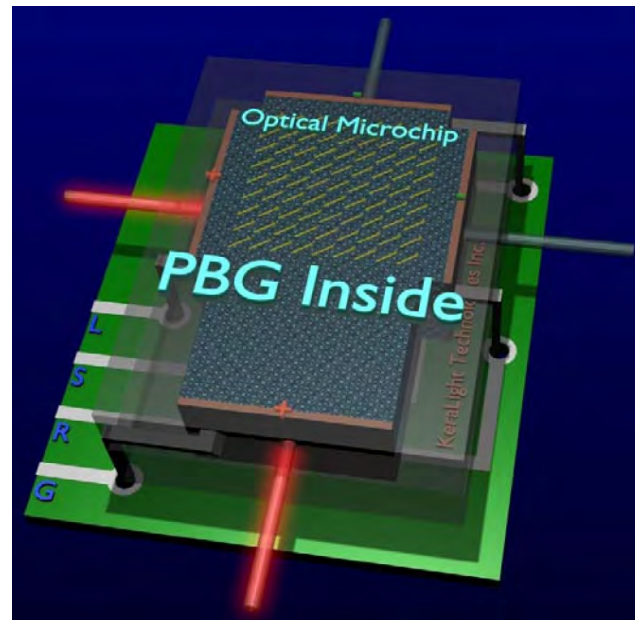
- **Custom designed electromagnetic vacuum**
- **Control of spontaneous emission**
- **Zero threshold lasers**
- **Ultrasmall optical components**
- **Ultrafast all-optical switching**
- **Integration of components on many layers**

# Visions for photonic crystals



## 'Photonic Micropolis'

J. Joannopoulos Research Group (MIT)  
<http://ab-initio.mit.edu/>



## 'Optical Microchip'

S. John Research Group (Toronto)  
<http://www.physics.utoronto.ca/~john/>